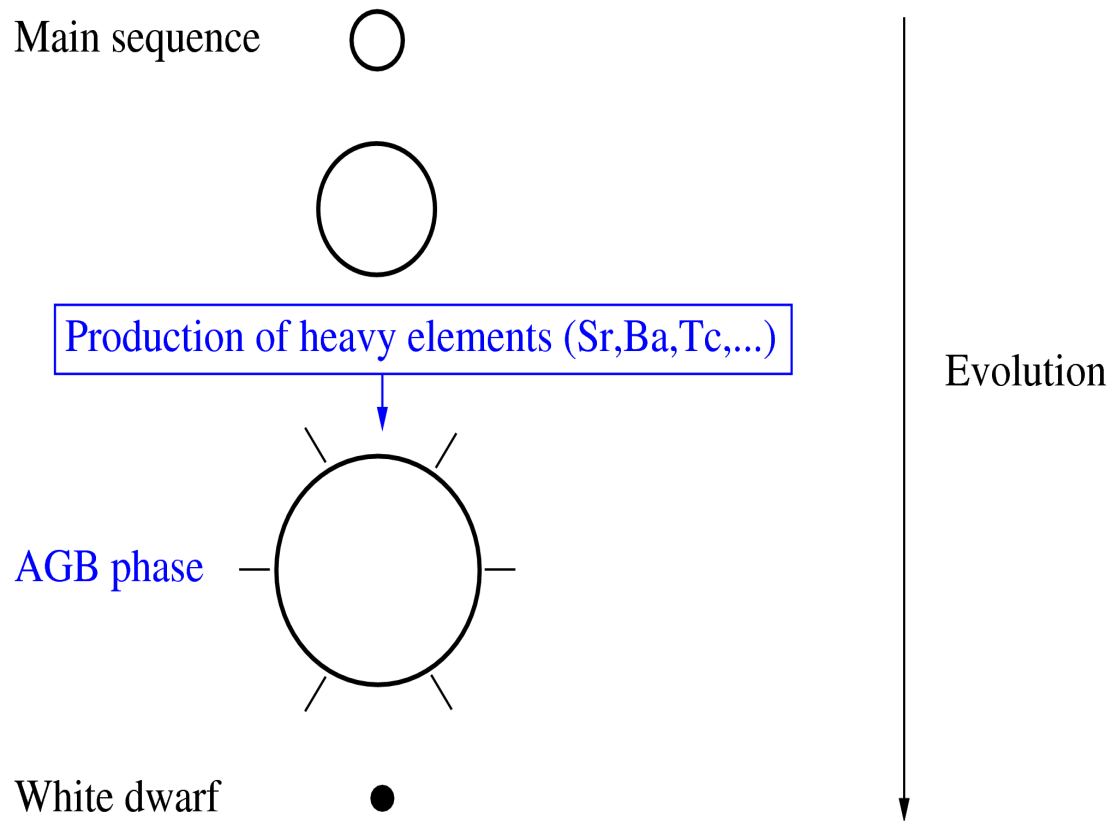


# RLOF stability revisited in case of AGB star mass loss

Dermine Tyl  
PhD student since October 2007

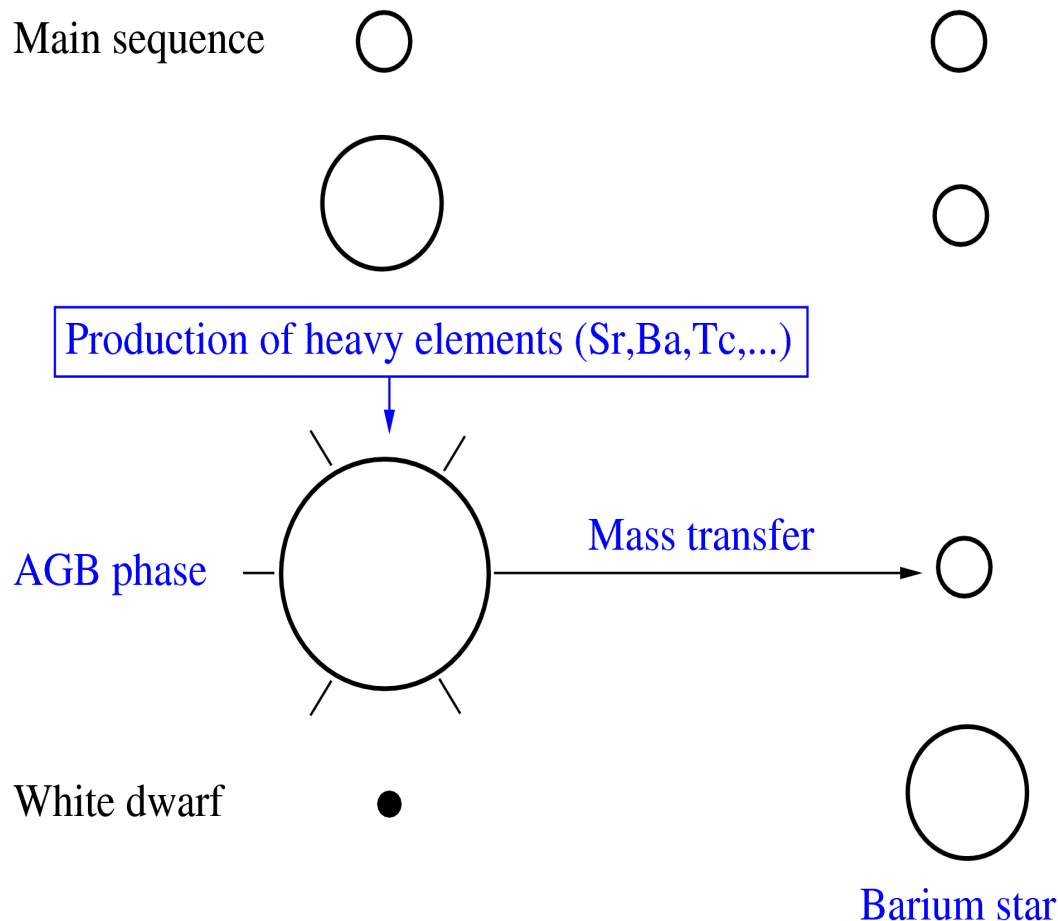
Promotor: A. Jorissen  
Co-promotor: L. Siess

# The post-mass transfer systems



- The AGB stars present a mass loss by wind.

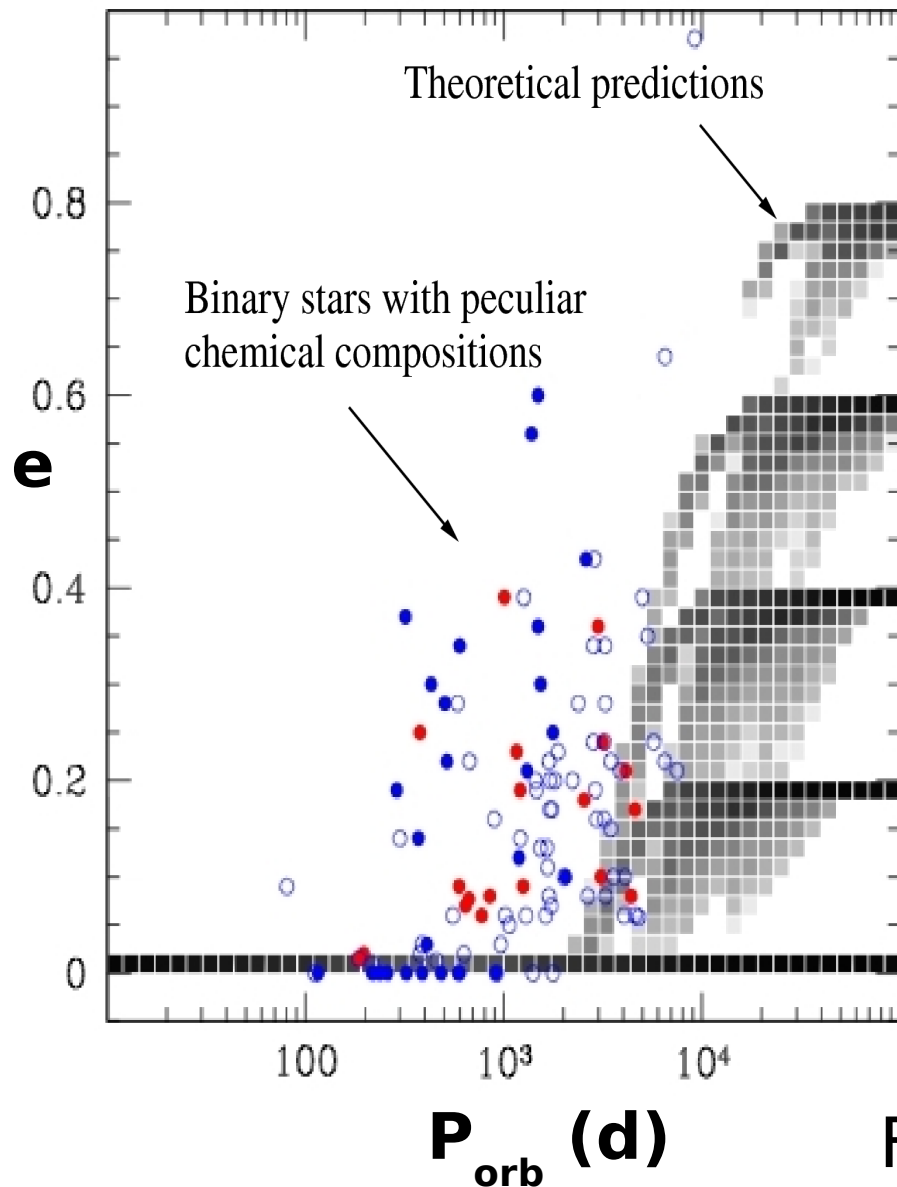
# The post-mass transfer systems



- The AGB stars present a mass loss by wind.

→ Accounts for the C and Ba “et al.” enrichment of some non-AGB stars in post-mass transfer binaries.

# The e-log $P_{\text{orb}}$ diagram



- AGB mass loss, mass transfer and tidal effect **lead the orbital evolution** of binaries.

But the orbital characteristics of many systems **resist to the explanation** by current theoretical models.

Frankowski (2007)

# PhD Project

- Simulate the evolution of orbital elements of binary systems by a theoretical model, the “**Transient torus**” (Frankowski & Jorissen 2007), which include:
  - Tidal effects
  - Mass transfer
    - by wind accretion
    - by RLOF
  - Pulsation of star
  - Disk-orbit interaction

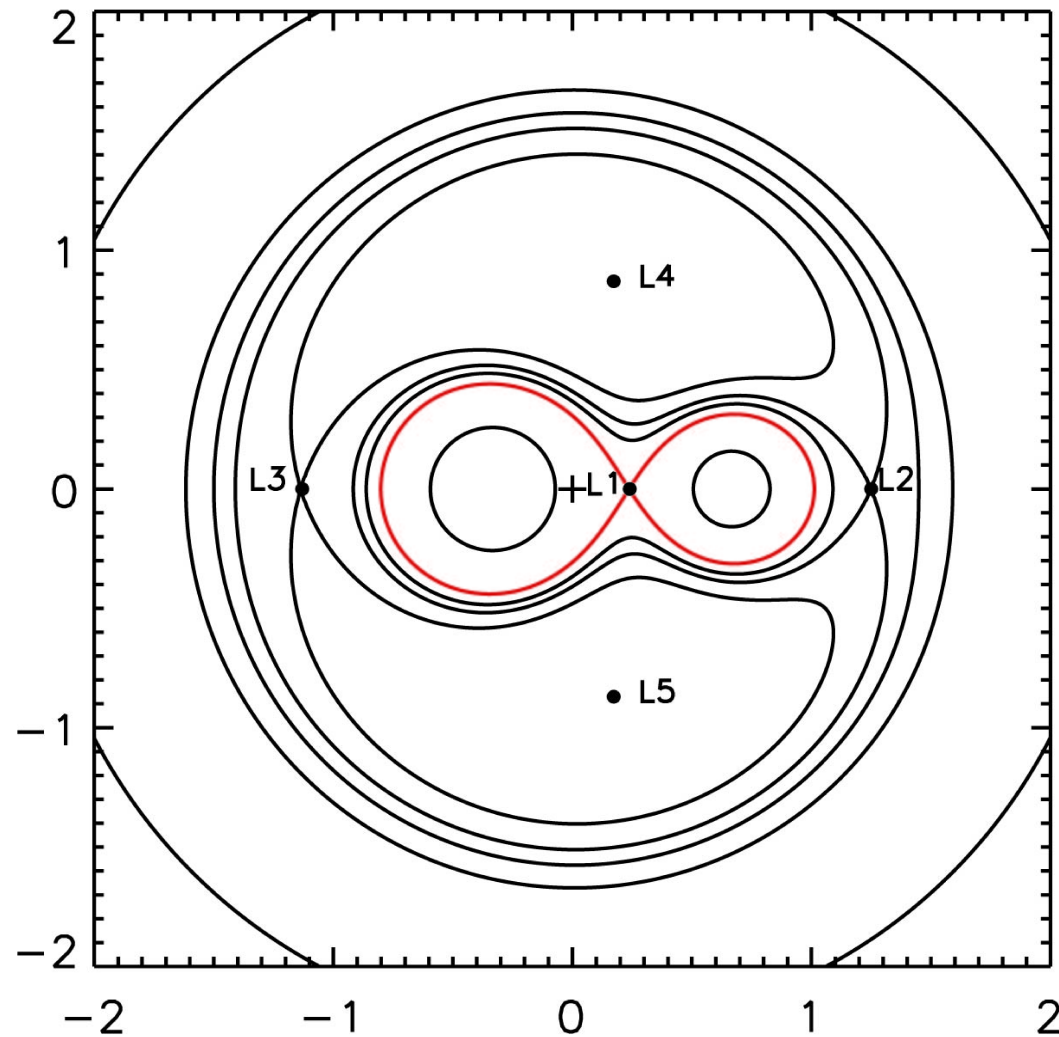
# PhD Project

- Simulate the evolution of orbital elements of binary systems by a theoretical model, the “**Transient torus**” (Frankowski & Jorissen 2007), which include:
  - Tidal effects
  - Mass transfer by wind accretion by RLOF
  - Pulsation of star
  - Disk-orbit interaction
- Observational hints:
  - **Large spin of the companion:**  
56 Peg (Frankowski & Jorissen 2006), HD 165141 (Jorissen et al. 1996), ...
  - **Presence of a circumbinary disk:**  
(Van Winckel 2003)

# PhD Project

- Simulate the evolution of orbital elements of binary systems by a theoretical model, the “**Transient torus**” (Frankowski & Jorissen 2007), which include:
  - Tidal effects
  - Mass transfer
    - by wind accretion
    - by **RLOF**
  - Pulsation of star
  - Disk-orbit interaction

# Roche potential



- In the case of circular orbits in corotation, the effective potential is given by:

$$\Phi = -\frac{\mu}{r_1} - \frac{1-\mu}{r_2} - \frac{x^2 + y^2}{2}$$

where

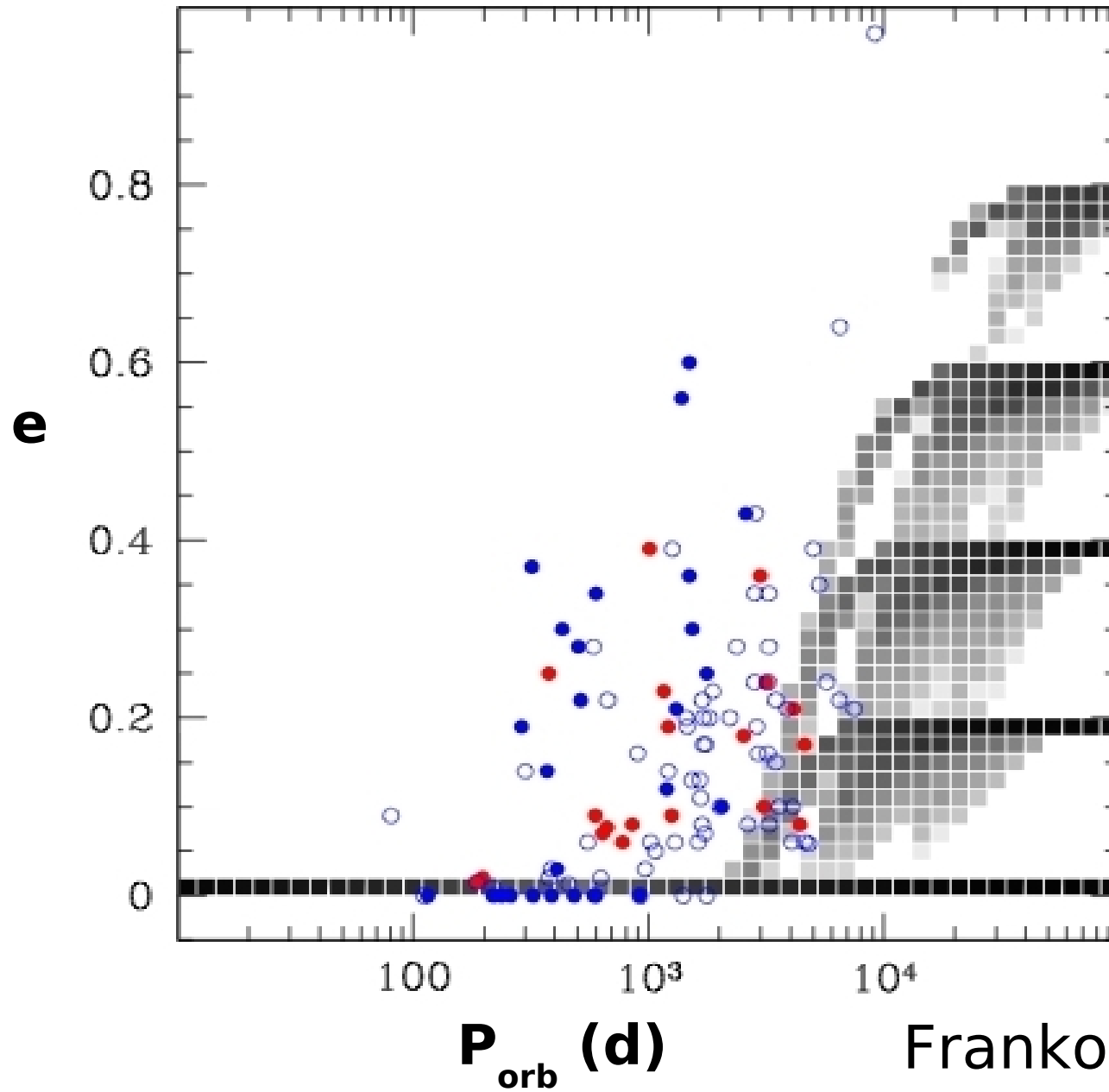
$$\mu = \frac{M_{AGB}}{M_{AGB} + M_2}$$

$$r_1 = \sqrt{(x+1-\mu)^2 + y^2 + z^2}$$

$$r_2 = \sqrt{(x-\mu)^2 + y^2 + z^2}$$



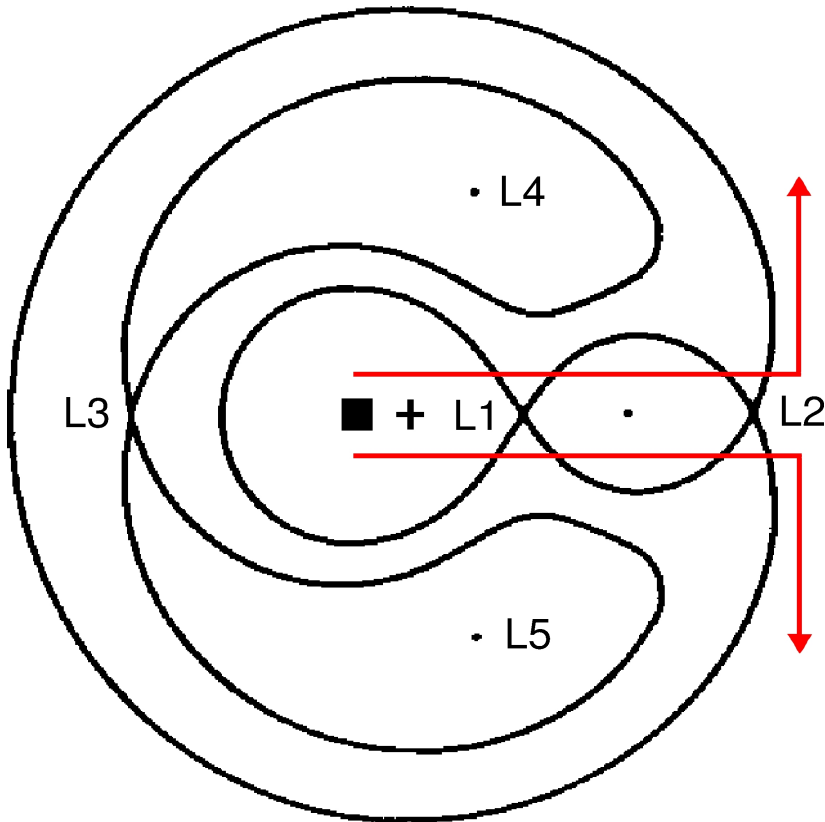
# The $e$ - $\log P_{\text{orb}}$ diagram



Frankowski (2007)

# Modified Roche potential

- By taking the radiation pressure on dust into account and the gaz/grains coupling:



Schuerman (1972)

$$f = \frac{\text{Radiation force}}{\text{Gravitational attraction}}$$

$$\Phi = -\frac{\mu(1-f)}{r_1} - \frac{1-\mu}{r_2} - \frac{x^2 + y^2}{2}$$

where

$$\mu = \frac{M_{AGB}}{M_{AGB} + M_2}$$

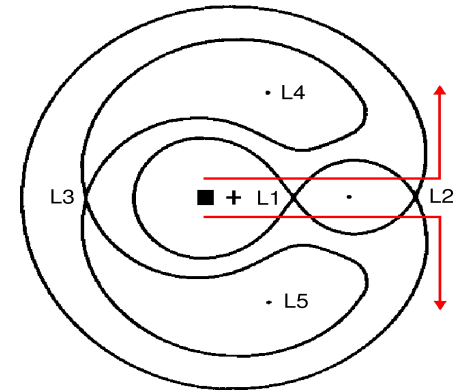
$$r_1 = \sqrt{(x+1-\mu)^2 + y^2 + z^2}$$

$$r_2 = \sqrt{(x-\mu)^2 + y^2 + z^2}$$

# Roche radius $R_R(q, f)$

- $f = \frac{\text{Radiation force}}{\text{Gravitational attraction}}$

$$\rightarrow \phi = -\frac{\mu(1-f)}{r_1} - \frac{(1-\mu)}{r_2} - \frac{x^2 + y^2}{2}$$



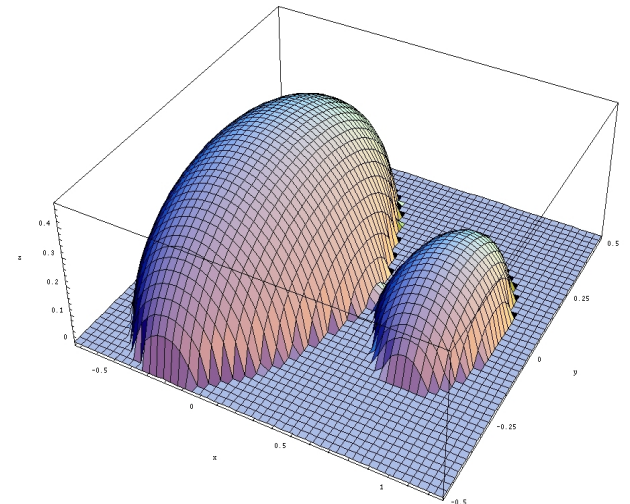
- Roche volumes for  $q = \left(\frac{M_{AGB}}{M_2}\right) \in [0, \infty]$  and  $f \in [0, 1]$ :

$$\frac{R_R(q, f)}{a} = \frac{A(f)q^{2/3}}{B(f)q^{2/3} + \log(1 + C(f)q^{1/3})}$$

$$C(f) = 1 + f$$

$$B(f) = 0.6(1 + 1/2f)$$

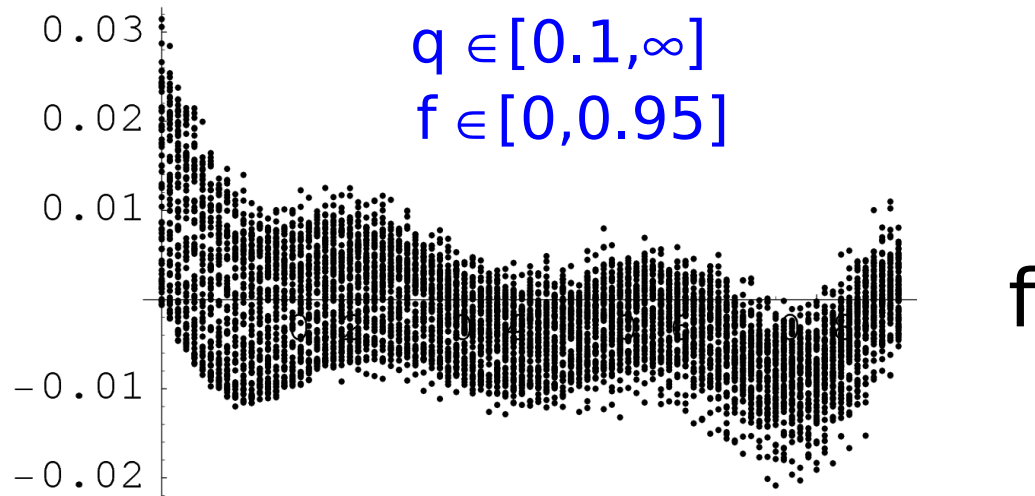
$$A(f) = 0.49 + 0.08f - 0.69f^2 + 12.81f^3 - 75.50f^4 + 208.14f^5 - 300.60f^6 + 219.70f^7 - 64.27f^8$$



# Precision of $R_R(q, f)$

- Numerical values are approximated by  $R_R(q, f)$ , to better than 3% over the range  $q \in [0.1, \infty]$  &  $f \in [0, 0.95]$

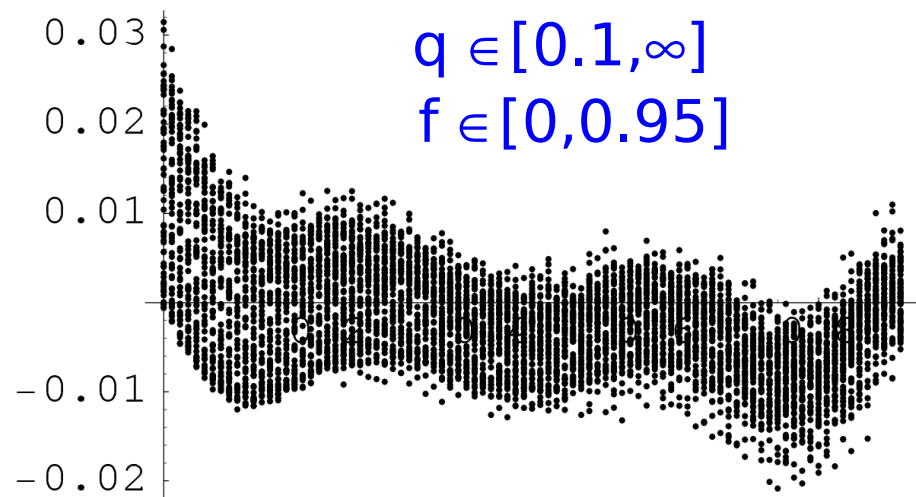
## Relative Error



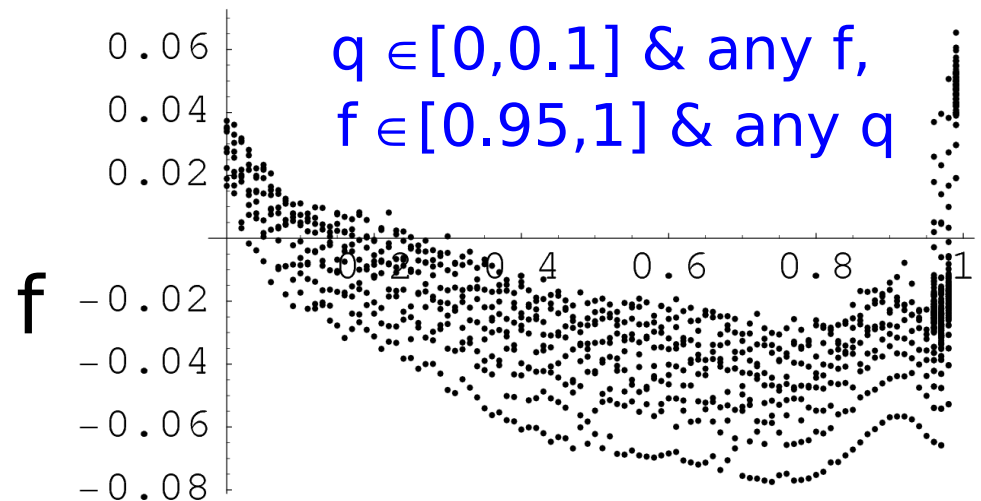
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Relative Error



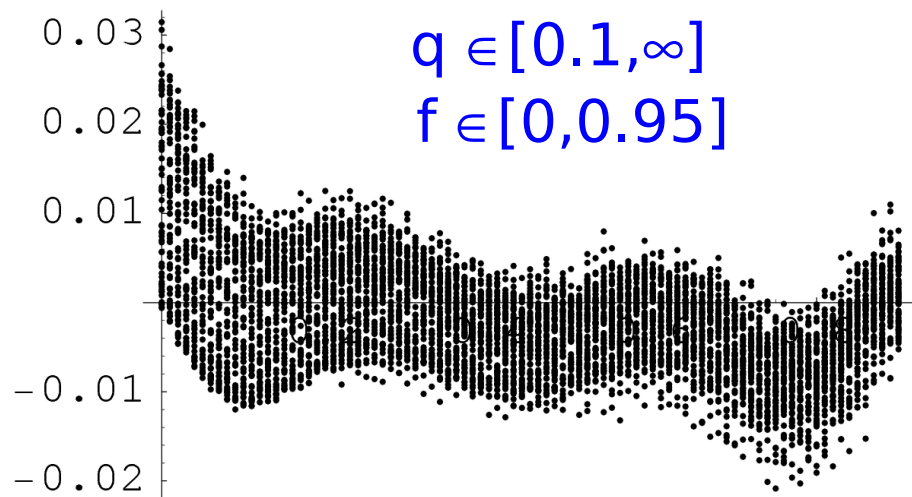
Relative Error



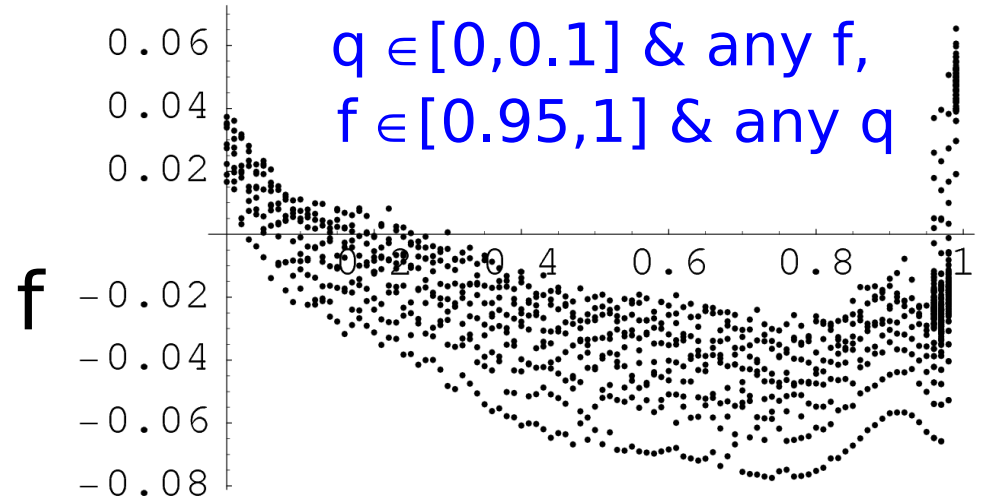
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Relative Error



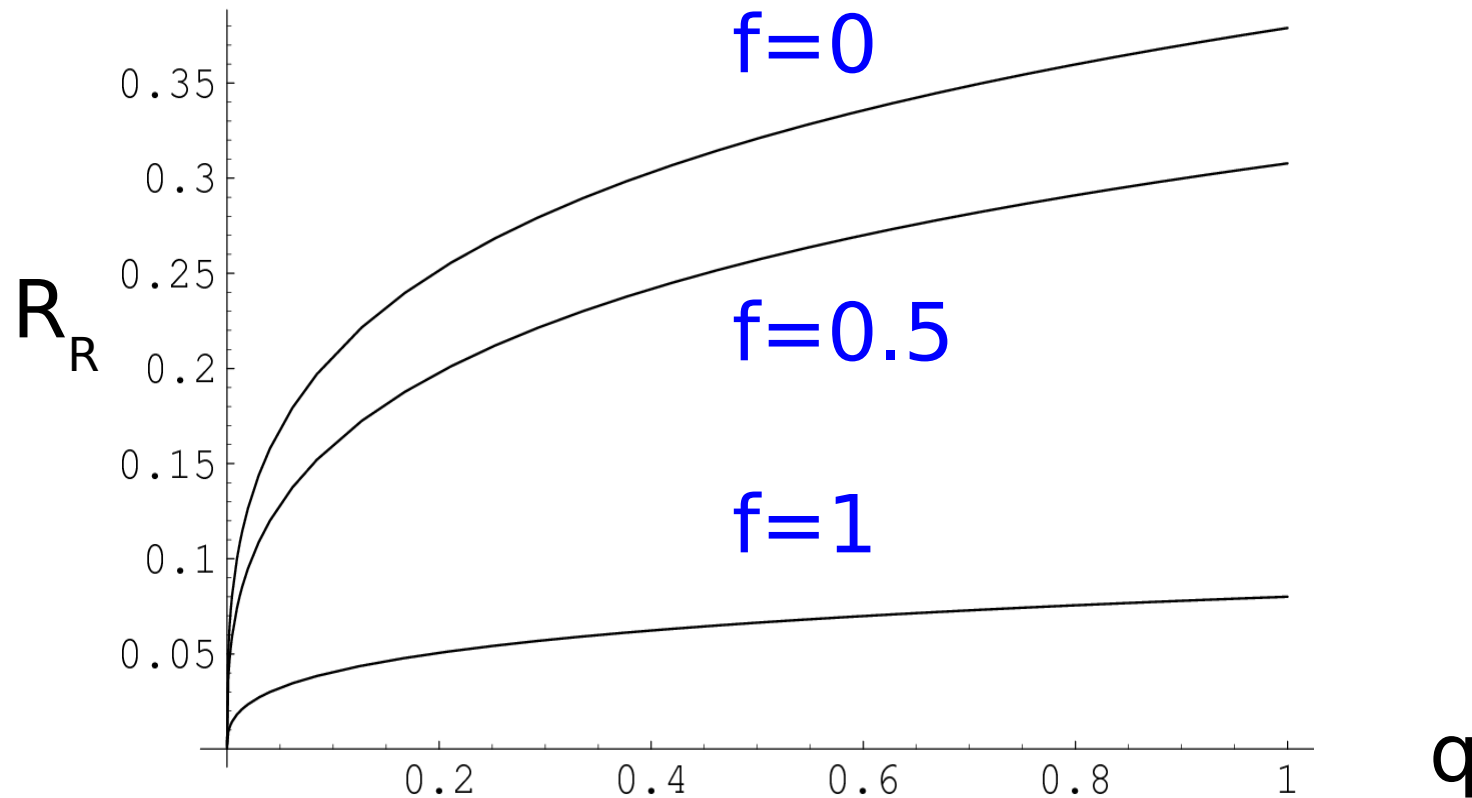
Relative Error



- $R_R(q, f=0) = R_R$  from Eggleton (1983)

# Roche radius $R_R(q, f)$

- $R_R \searrow$  by a factor  $\sim 5$  from  $f=0$  to  $f=1$ .



→ Important modifications of the binary evolution

# Astrophysics application

1.  $R_R \searrow$  by a factor  $\sim 5$  from  $f=0$  to  $f=1$ .

→ could be a solution for the too high predicted Roche radius of some symbiotic stars (Mikolajewska (2007)):

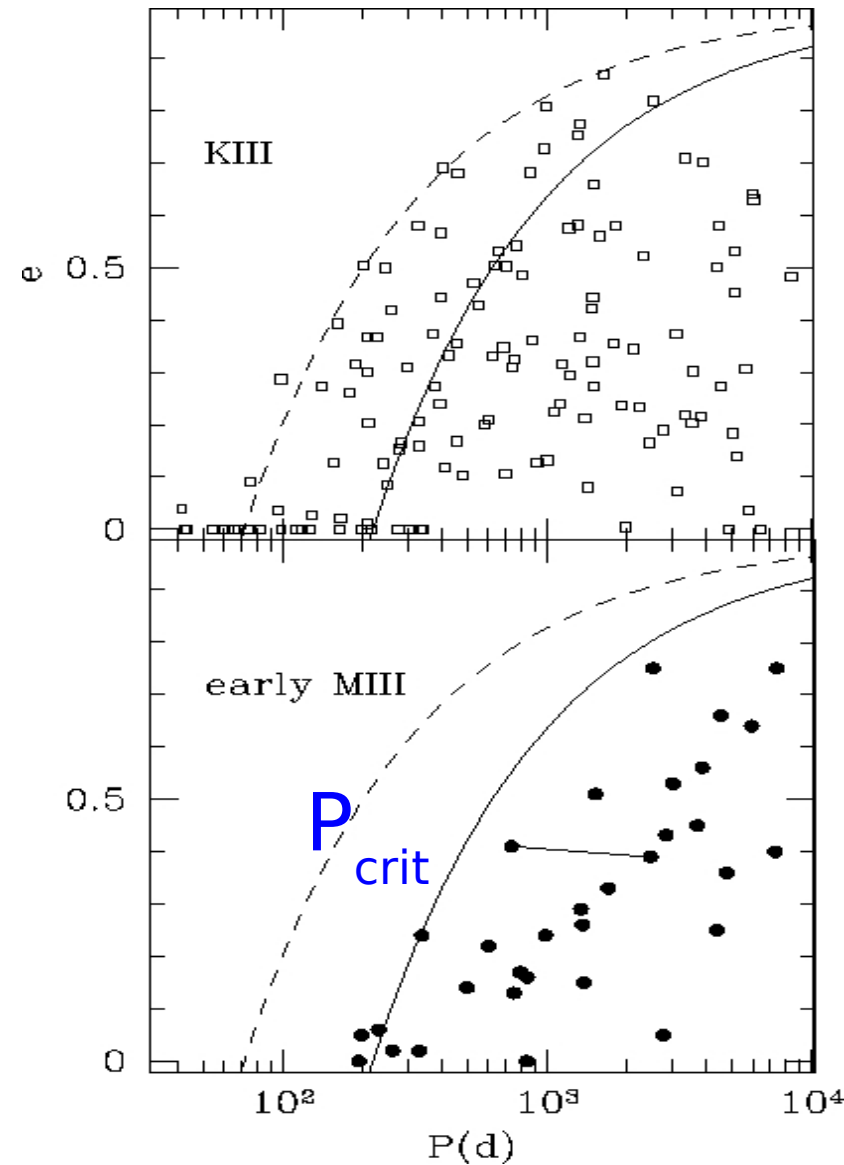
Ellipsoidal variations **only if  $R/R_R > 0.8$**

Mikolajewska find  **$R/R_R = 0.5$**



# Astrophysics application

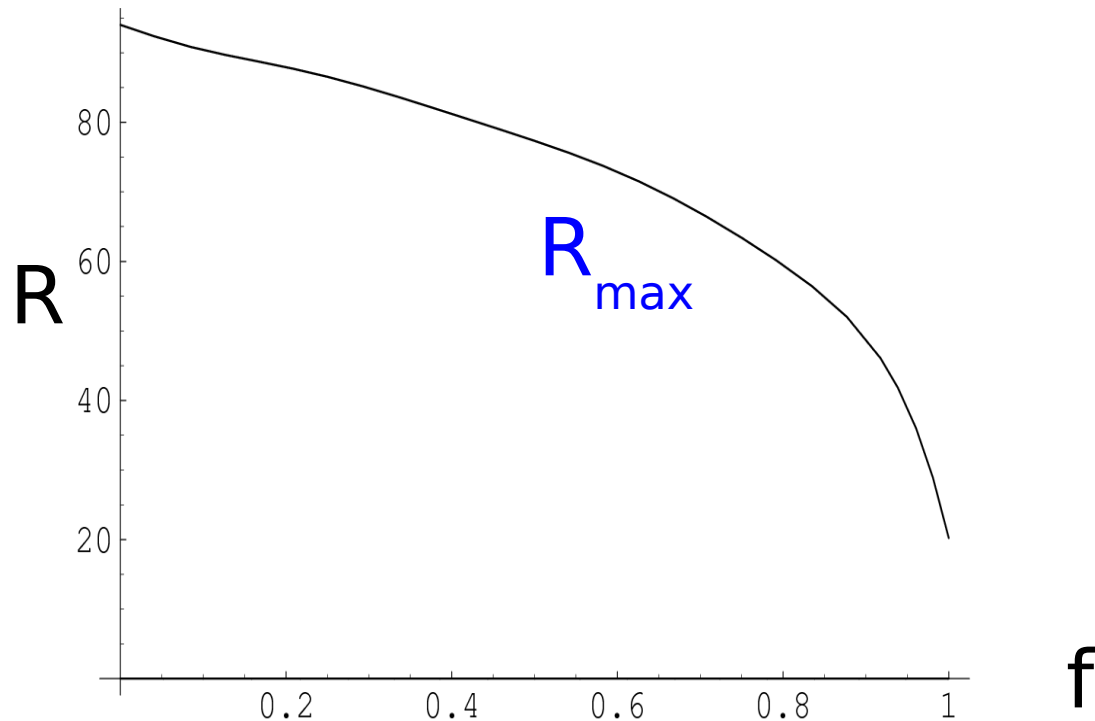
2.  $P_{\text{crit}}$ , the period below which the RLOF appears,  $\nearrow$  by a factor  $\sim 10$  from  $f=0$  to  $f=1$ .



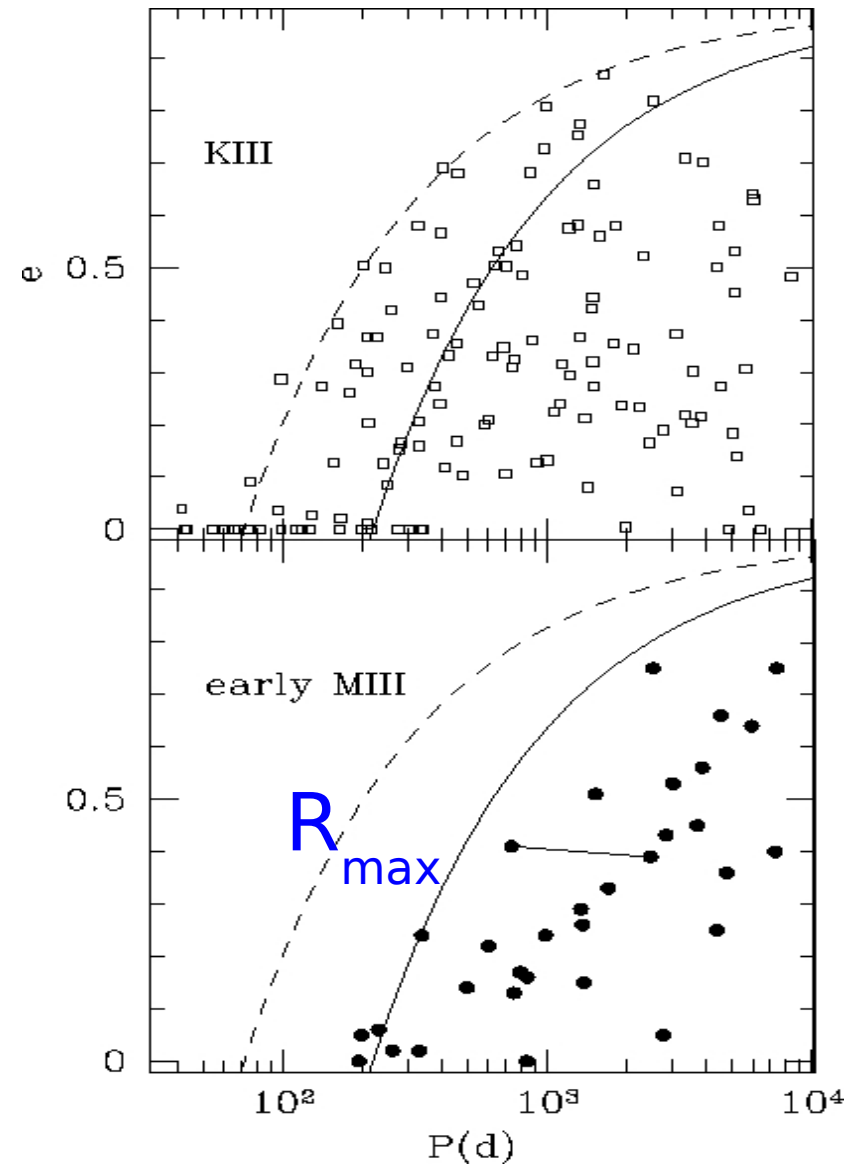
Mermilliod et al. (2007)  
Jorissen et al. (2008)

# Astrophysics application

2.  $P_{\text{crit}}$ , the period below which the RLOF appears,  $\nearrow$  by a factor  $\sim 10$  from  $f=0$  to  $f=1$ .



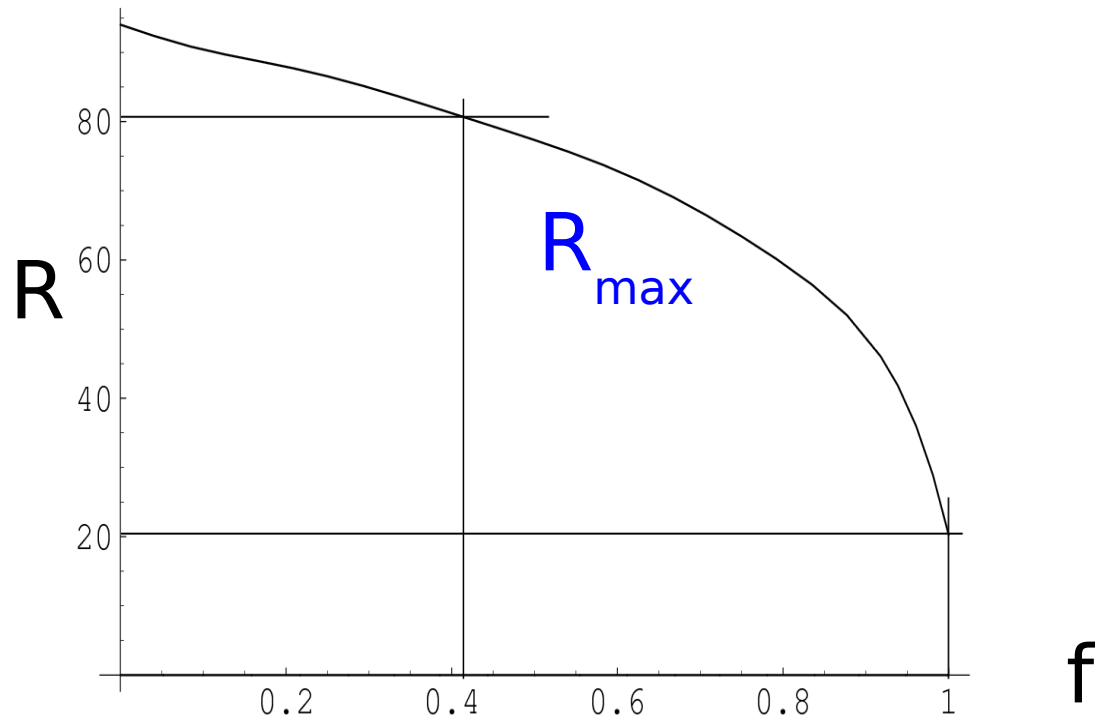
For  $M=M_1+M_2=1.9 M_{\odot}$



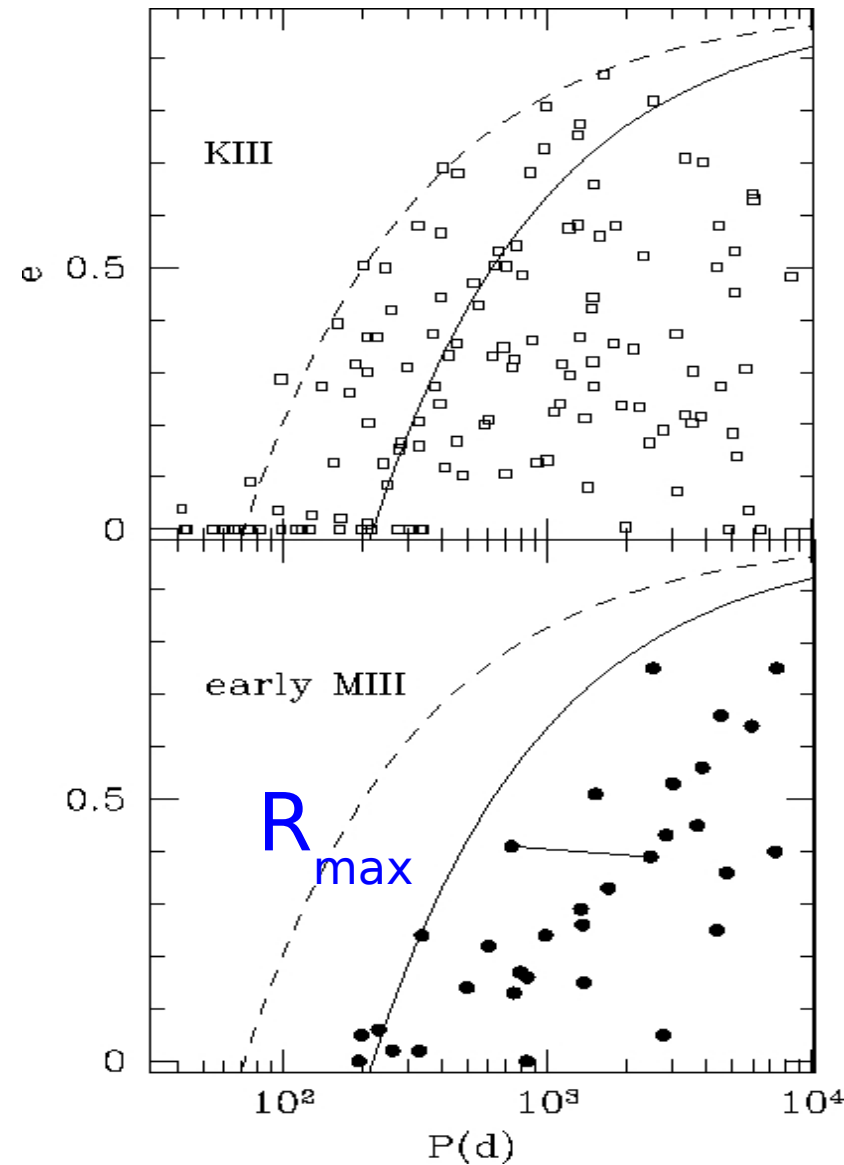
Mermilliod et al. (2007)  
Jorissen et al. (2008)

# Astrophysics application

2.  $P_{\text{crit}}$ , the period below which the RLOF appears,  $\nearrow$  by a factor  $\sim 10$  from  $f=0$  to  $f=1$ .



$R \in [20, 80R_{\odot}]$  for M0 stars  
(Dumm & Schild 1998)



Mermilliod et al. (2007)  
Jorissen et al. (2008)

# Conclusions

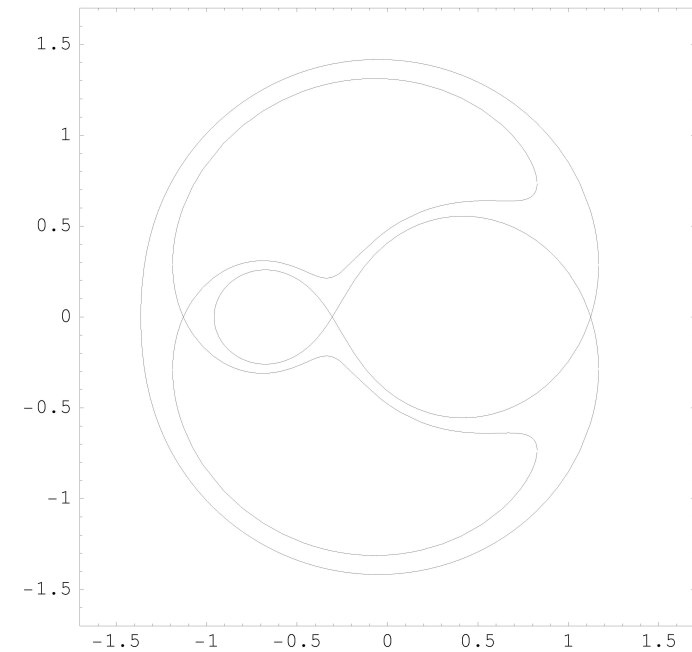
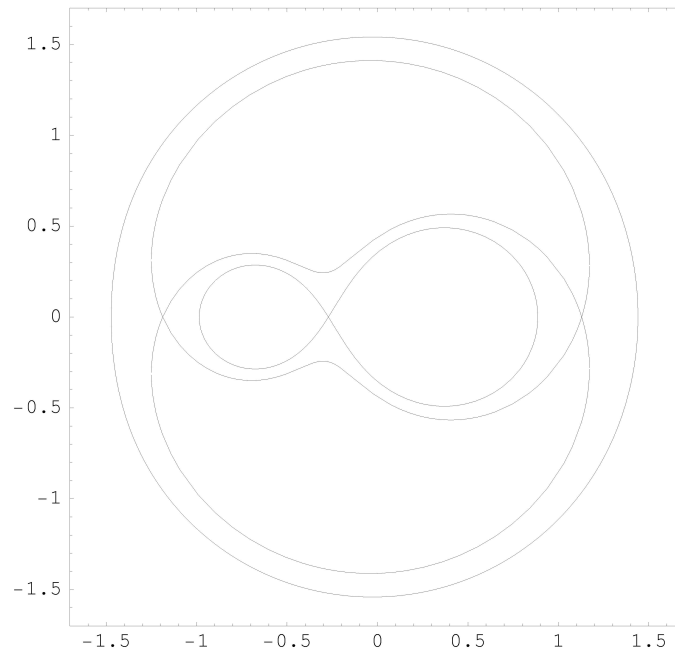
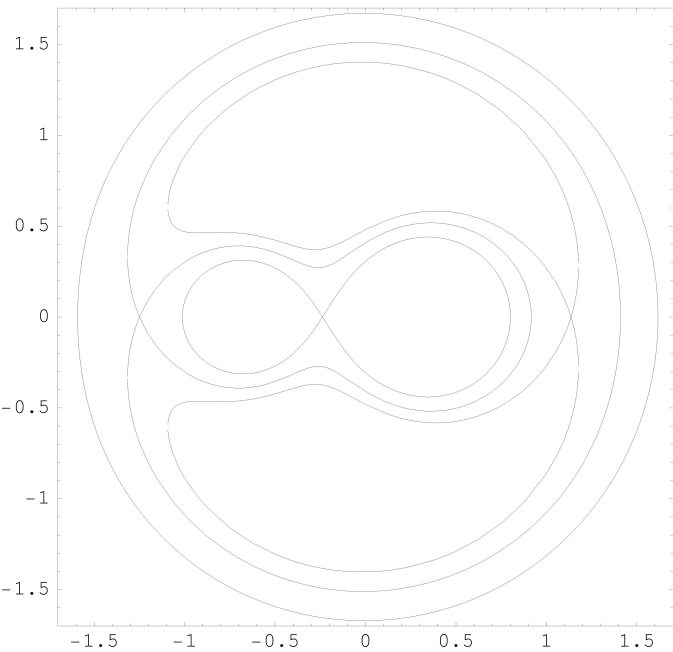
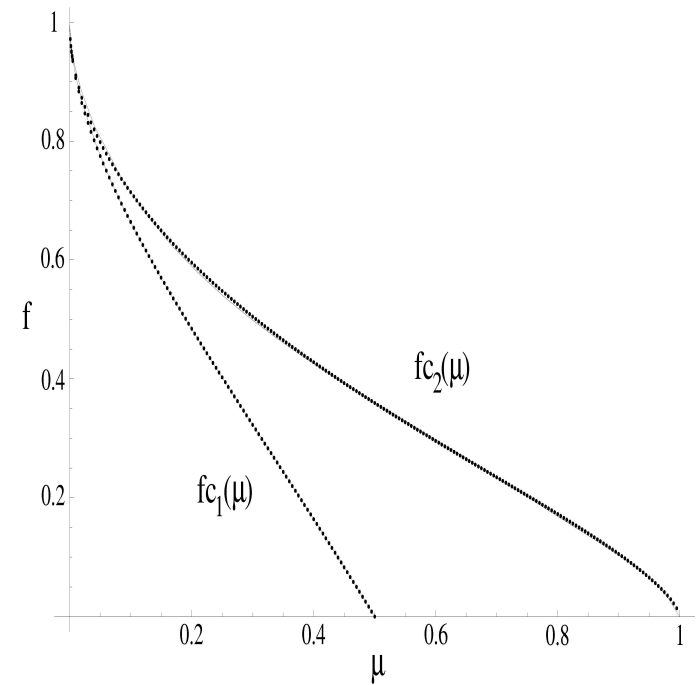
- $P_{\text{rad}}$  is not negligible.
- The value of  $f$  can be near of 1.
- Have an important impact on the evolution of post-mass transfer binaries.

# Annexes

# Modified Roche potential

$$\phi = \frac{\mu(1-f)}{r_1} - \frac{(1-\mu)}{r_2} - \frac{x^2+y^2}{2}$$

- $fc_1(q)$ :  $L_1$  &  $L_3$  share the same equipotential.
- $fc_2(q)$ :  $L_2$  &  $L_3$  share the same equipotential.



RLOF stability

# Study of RLOF Stability

$$R_{AGB}(t_0 + \Delta t) = R_{AGB}(t_0) + \frac{dR_{AGB}}{dM} \frac{dM}{dt} \Delta t, \quad R_R(t_0 + \Delta t) = R_R(t_0) + \frac{dR_R}{dM} \frac{dM}{dt} \Delta t$$

$$\zeta_{AGB} = \frac{d \ln R_{AGB}}{d \ln M}, \quad \zeta_R = \frac{d \ln R_R}{d \ln M}$$

Stability condition: *If*  $R_{AGB}(t_0) < R_R(t_0) \Rightarrow R_{AGB}(t_0 + \Delta t) < R_R(t_0 + \Delta t)$

$$\Rightarrow \zeta_R < \zeta_{AGB}$$

→ Improvement of  $\zeta_R$  and  $\zeta_{AGB}$



# $\zeta_R(q, f)$

$$\zeta_R(q, f) = 2 \left( -\lambda + \frac{1 - \eta - \delta}{1 + q} + \gamma \delta (1 + q) \right) + \frac{q}{1 + q} (1 - \eta) + 2(\eta q - 1) + \frac{d \ln R_R(q, f) / a}{d \ln q} (1 + \eta q)$$

- Where,
  - $\alpha$  = fraction of the mass loss escaped to infinity
  - $\eta$  = fraction of the mass loss accreted by the companion
  - $\delta$  = fraction of the mass loss which form a circumbinary disk
  - $\lambda$  = drag exerted by the escaping wind on the orbital motion

# Obtaining $\zeta_R(q, f)$

- $\zeta_R = \dots + \frac{d \ln R_R}{d \ln q}$

↑  
Linked to the geometry of the Roche lobe.

Linked to the variations of the angular momentum associated with the mass loss.

# Obtaining $\zeta_R(q, f)$

- $\zeta_R = \dots + \frac{d \ln R_R}{d \ln q}$   
↓  
 $\frac{d \ln R_R}{d \ln q} \nearrow$  of  $\sim 10\%$  from  $f=0$  to  $f=1$ .

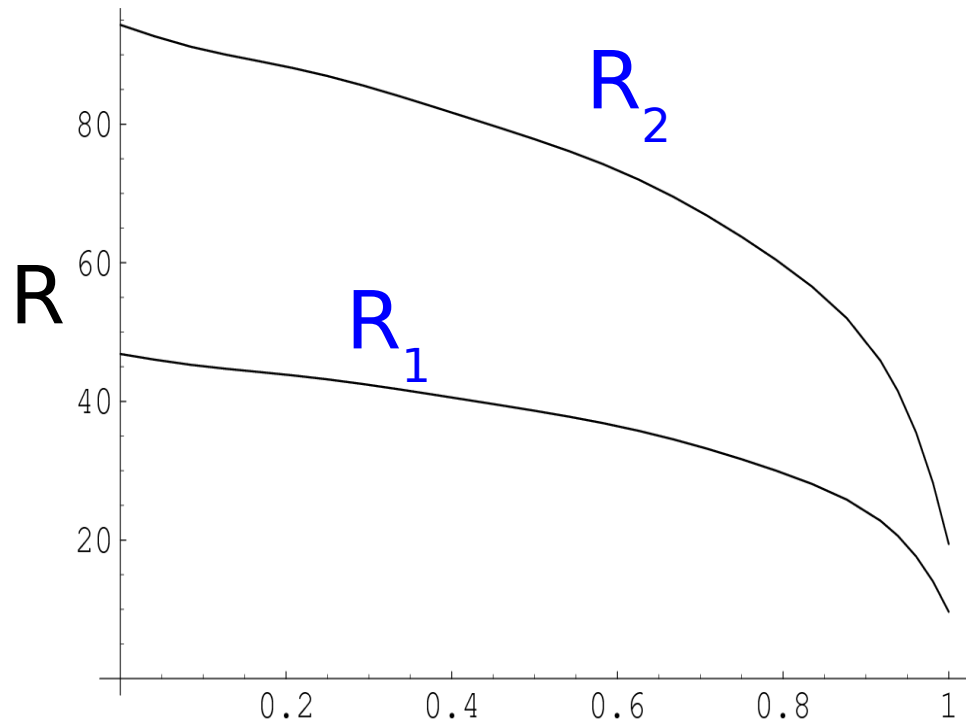
$\Rightarrow$  destabilize the system ( $\zeta_R < \zeta_{\text{AGB}}$ ).

- If the companion accretes all the mass loss,  $\zeta_R \nearrow$  of  $\sim 1\%$  from  $f=0$  to  $f=1$ .

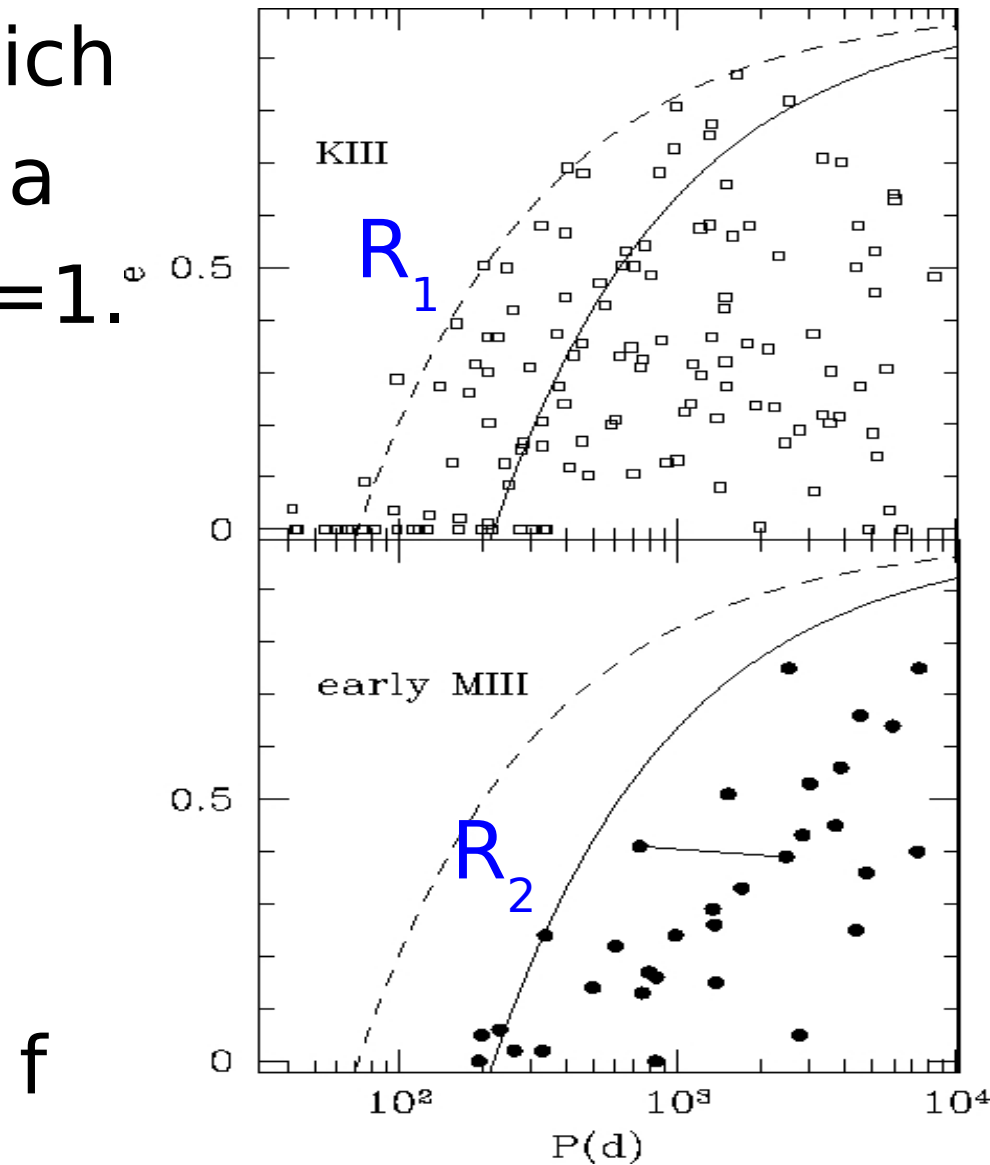
Rmax for MIII & KIII

# Roche radius $R_R(q, f)$

- $P_{\text{crit}}$ , the period below which the RLOF appears,  $\nearrow$  by a factor  $\sim 10$  from  $f=0$  to  $f=1$ .



For  $M = M_1 + M_2 = 1.9 M_\odot$

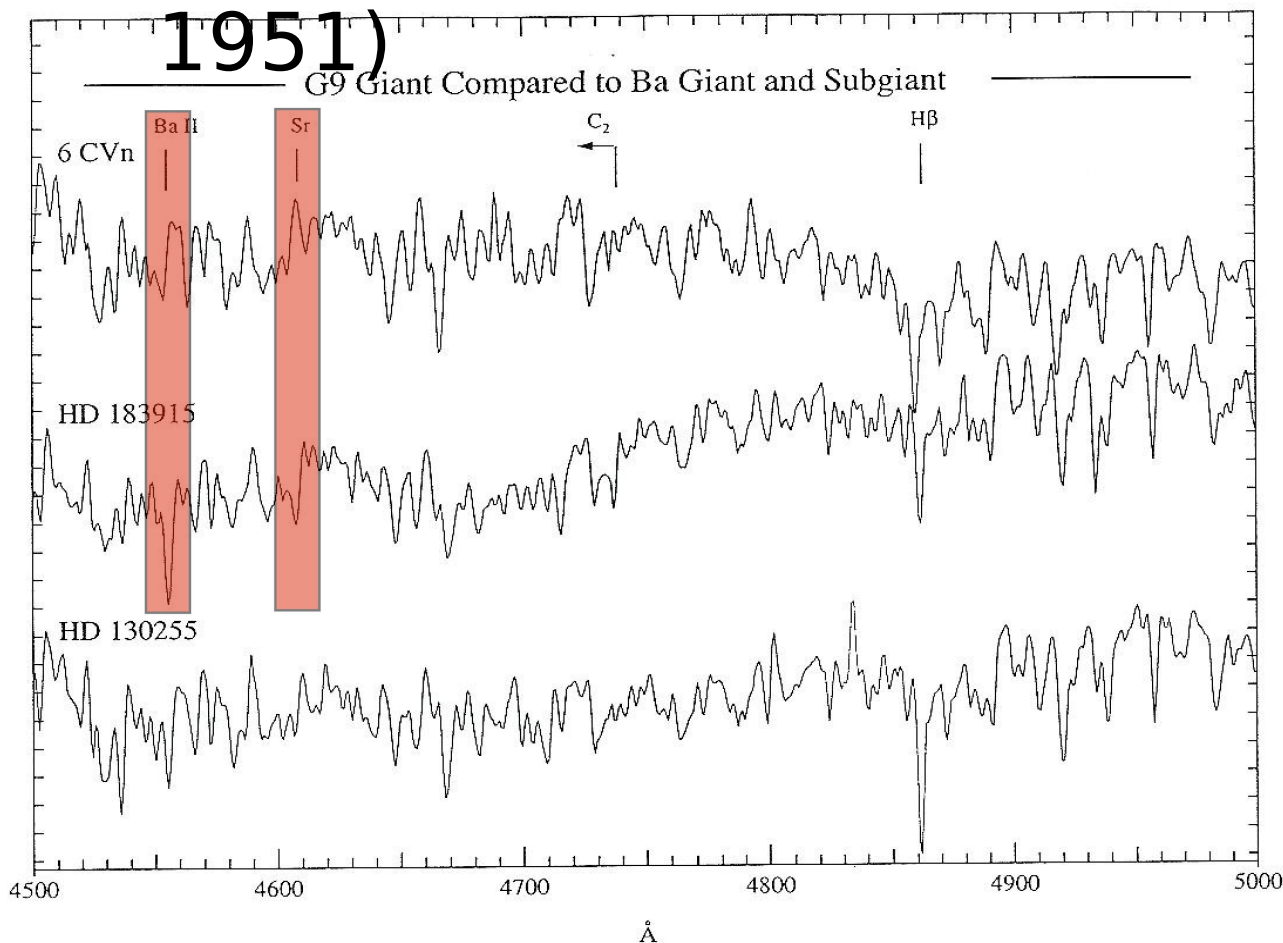


Mermilliod et al. (2007)

Jorissen et al. (2008)

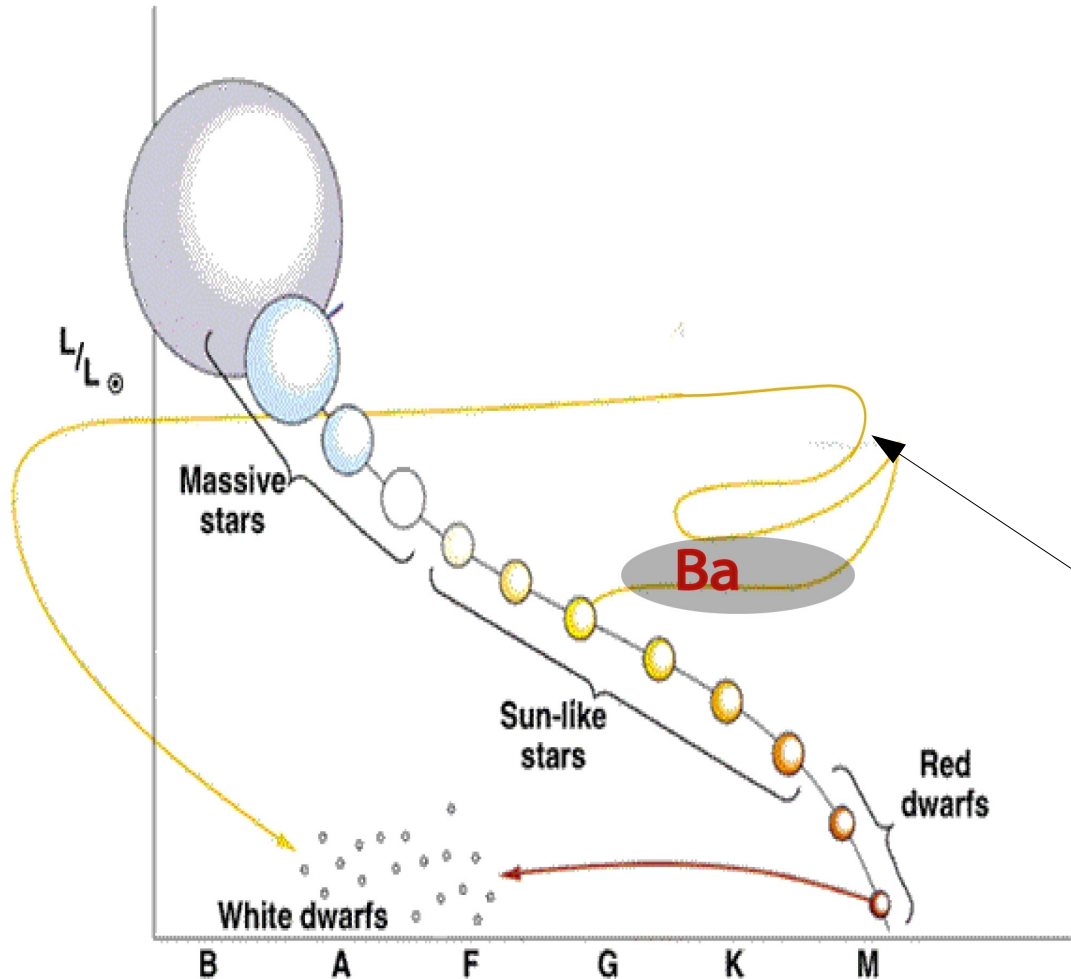
# Le cas des étoiles à Ba

- Découverte d'étoiles à baryum (Bidelman & Keenan



- Étoile 1: G9 III normale
- Étoile 2: K0 III Ba3.5
- Étoile 3: G9 IV Ba2

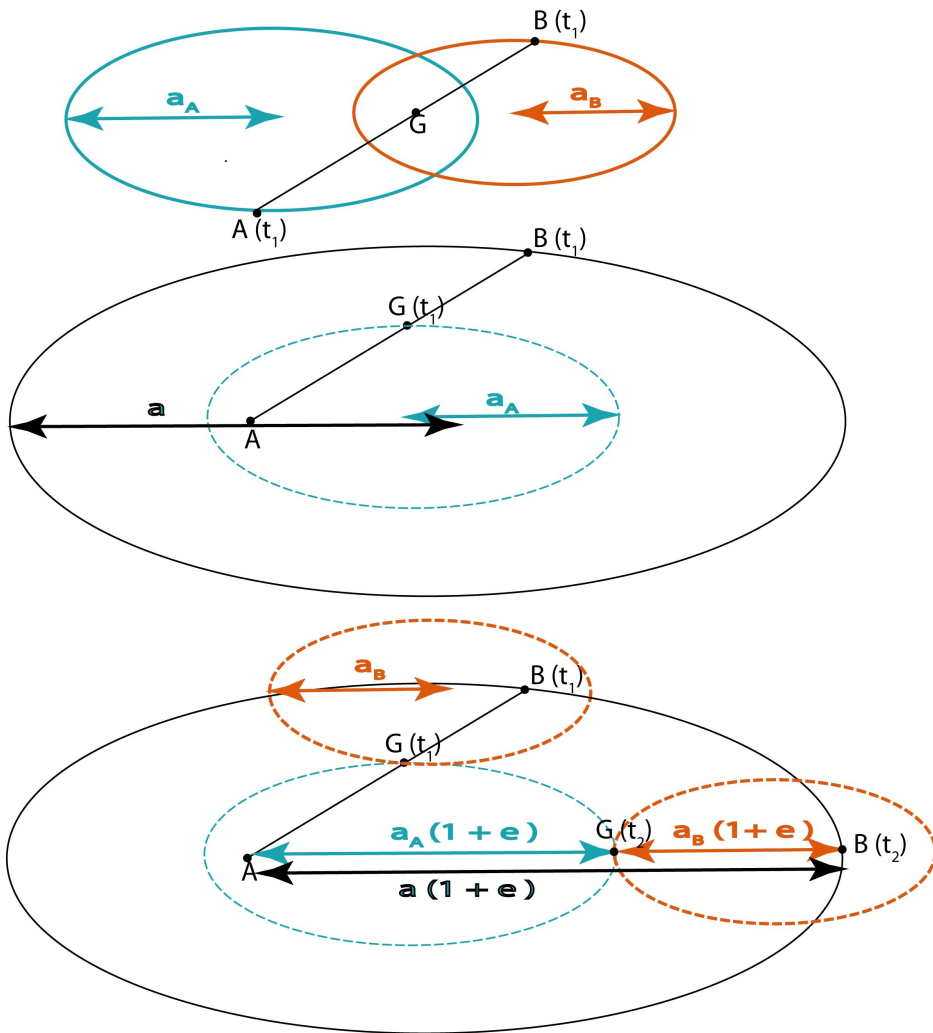
# Le cas des étoiles à Ba



- Ces étoiles à Ba proviennent de la RGB.

Mais le processus s a lieu dans les étoiles AGB ...

# Orbites



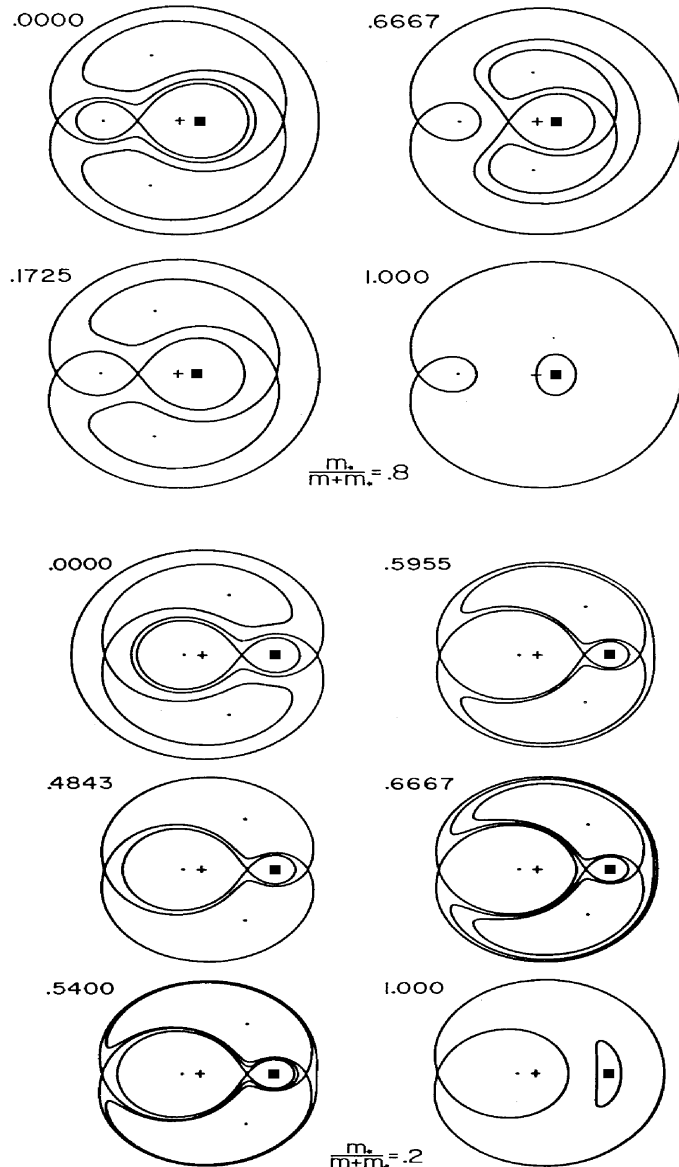
- Orbite absolue

- Orbite relative

- $a = a_A + a_B$   
 $a_A M_A = a_B M_B$  (déf de  $G$ )



# Potentiel de Roche modifié

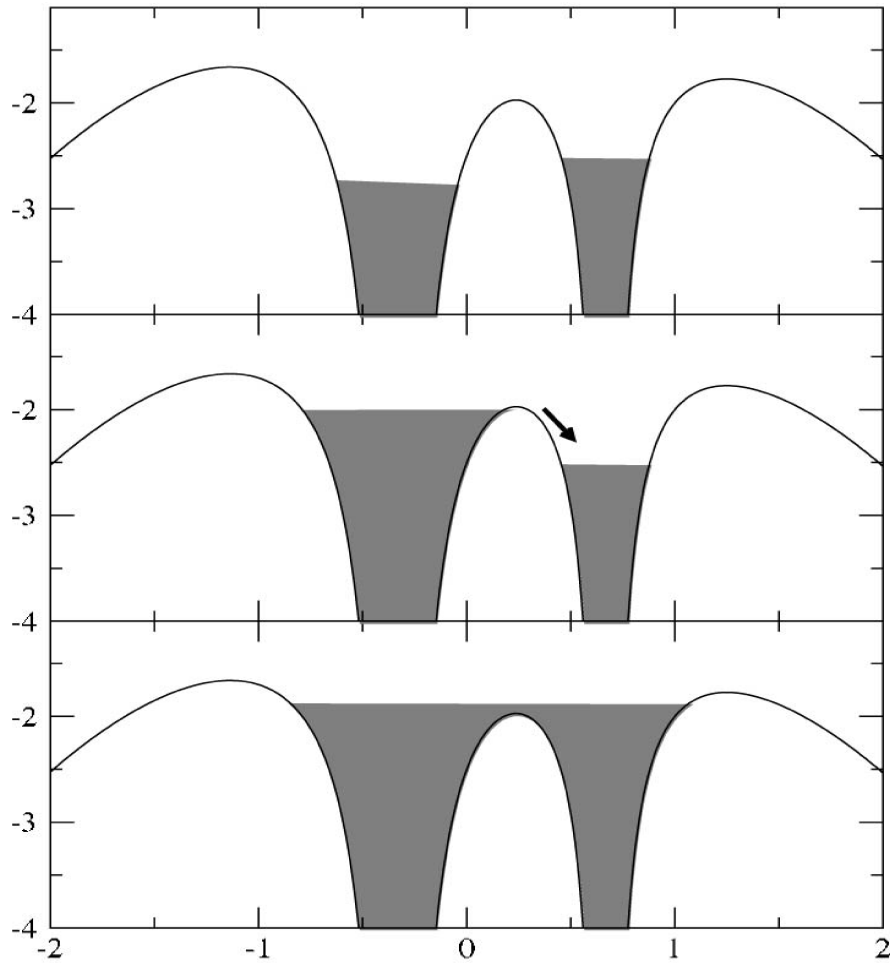


- Potentiel gravitationnel de 2 points massifs en corotation autour d'une orbite relative circulaire.

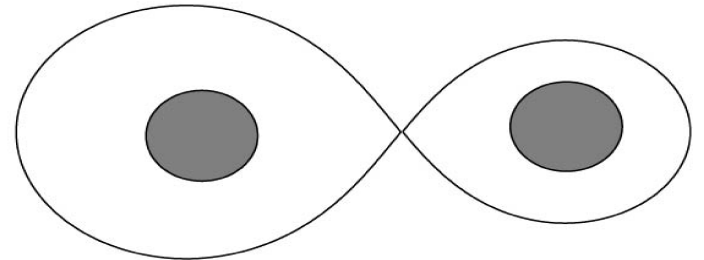
$$\phi = -\frac{\mu}{r_1} - \frac{(1-\mu)(1-f)}{r_2} - \frac{x^2 + y^2}{2}$$

$$f = \frac{-dP_{rad}}{\rho dr} \left( \frac{GM_2}{r_2^2} \right)^{-1}$$

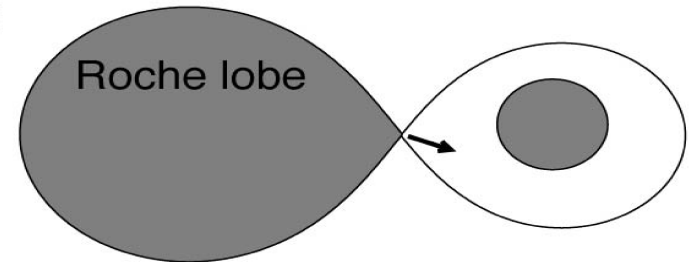
# Types de binaire



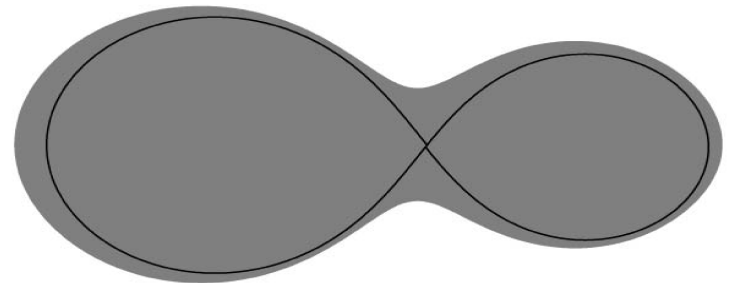
detached



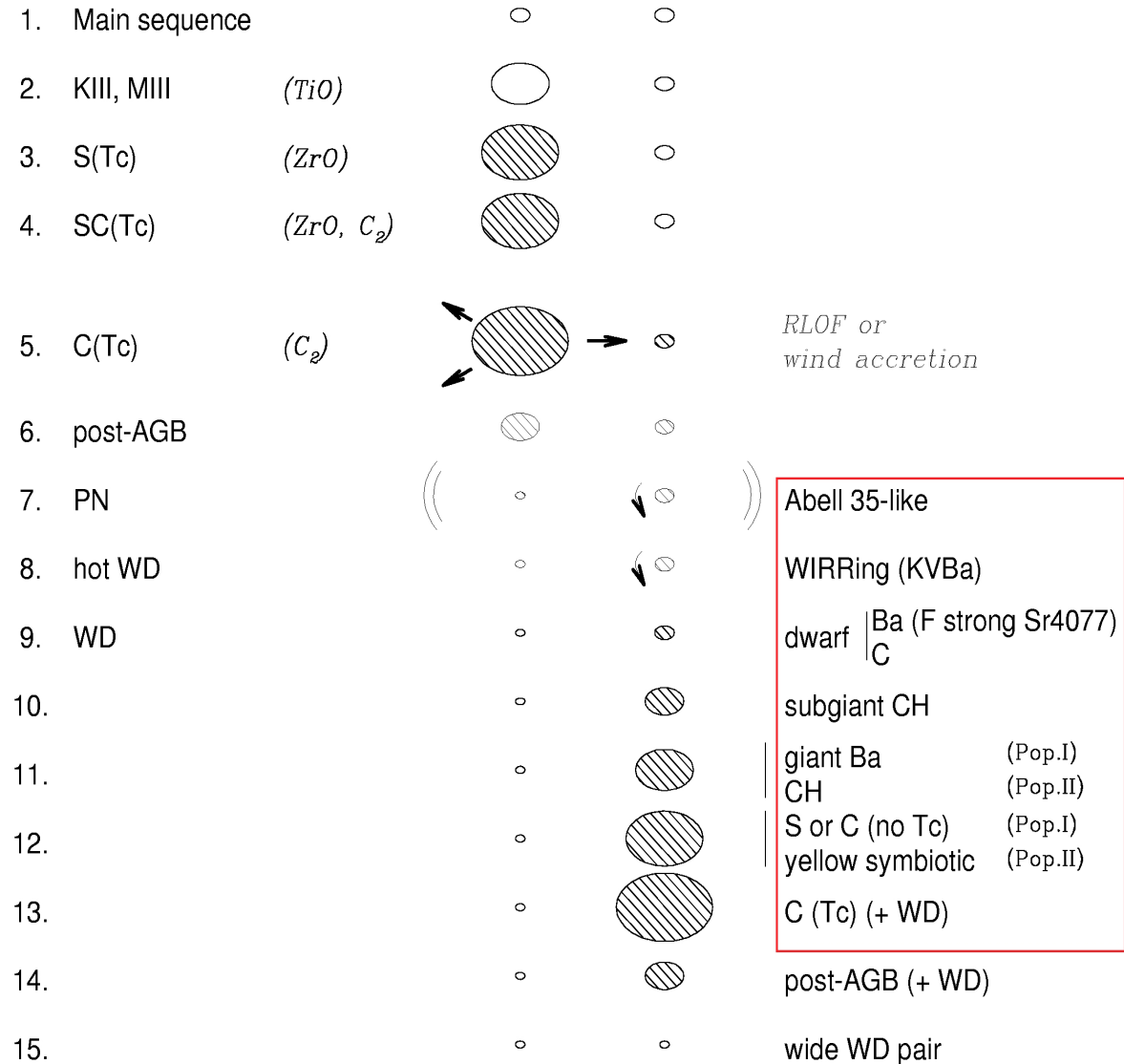
semi-detached  
mass transfer  
(RLOF)



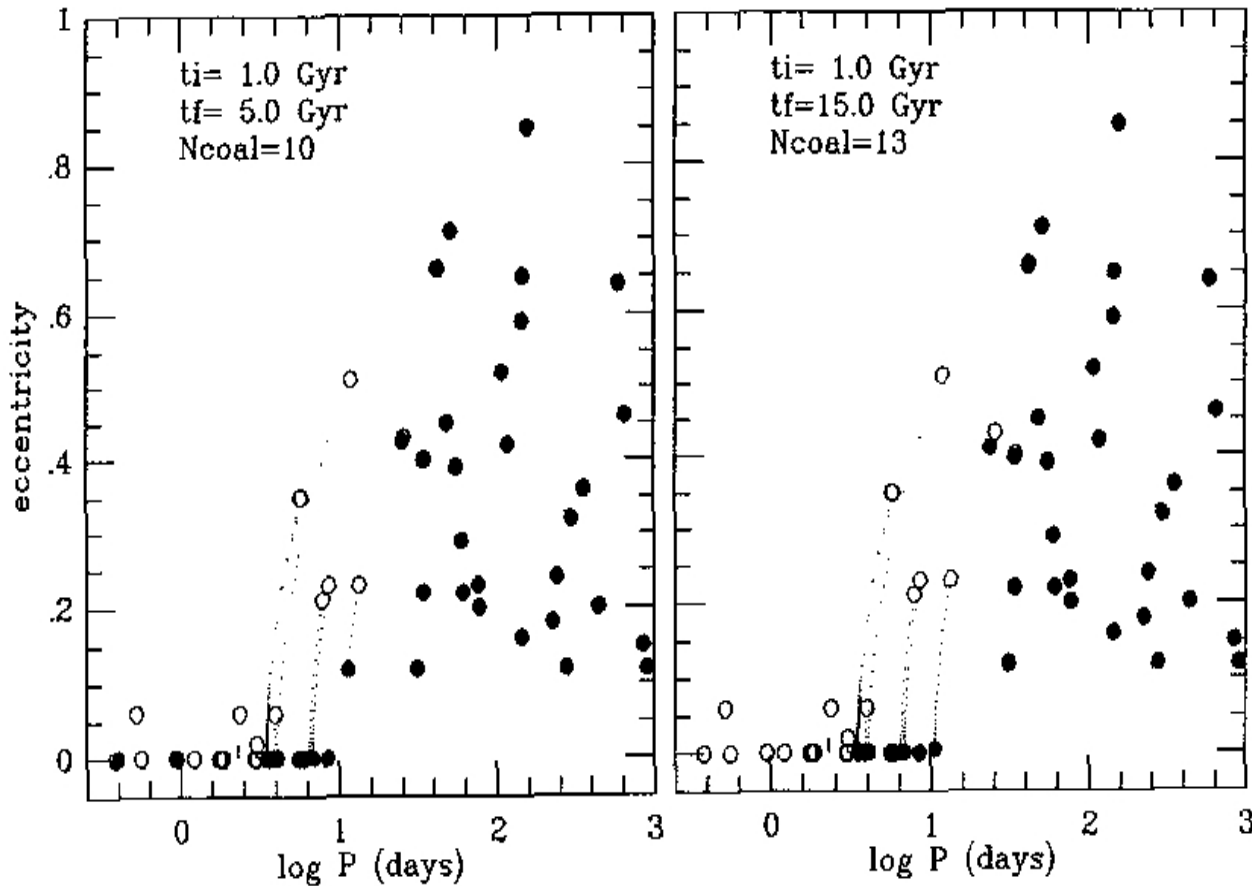
common  
envelope



# Évolution schématique



# Interaction de marée



- Circularisation:  
 $e \rightarrow 0$
- Synchronisation

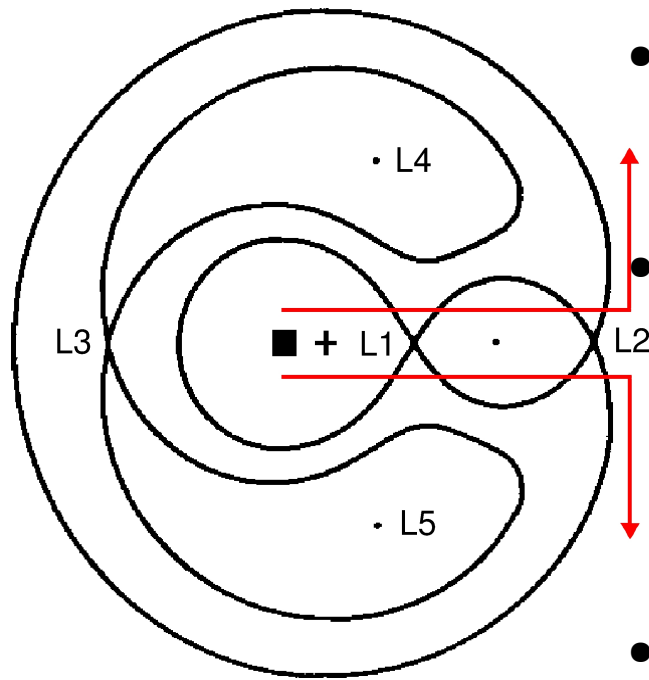
A. Duquennoy & M.  
Mayor

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# The transient torus

- 1: Wind accretion  
→ Important spin of the companion



- 2: Roche lobe overflow
- 3: Formation of a circumbinary torus by escaping matter through L2
- 4: Formation of a **Keplerian disk**

Schuerman (1996)

observational confirmations

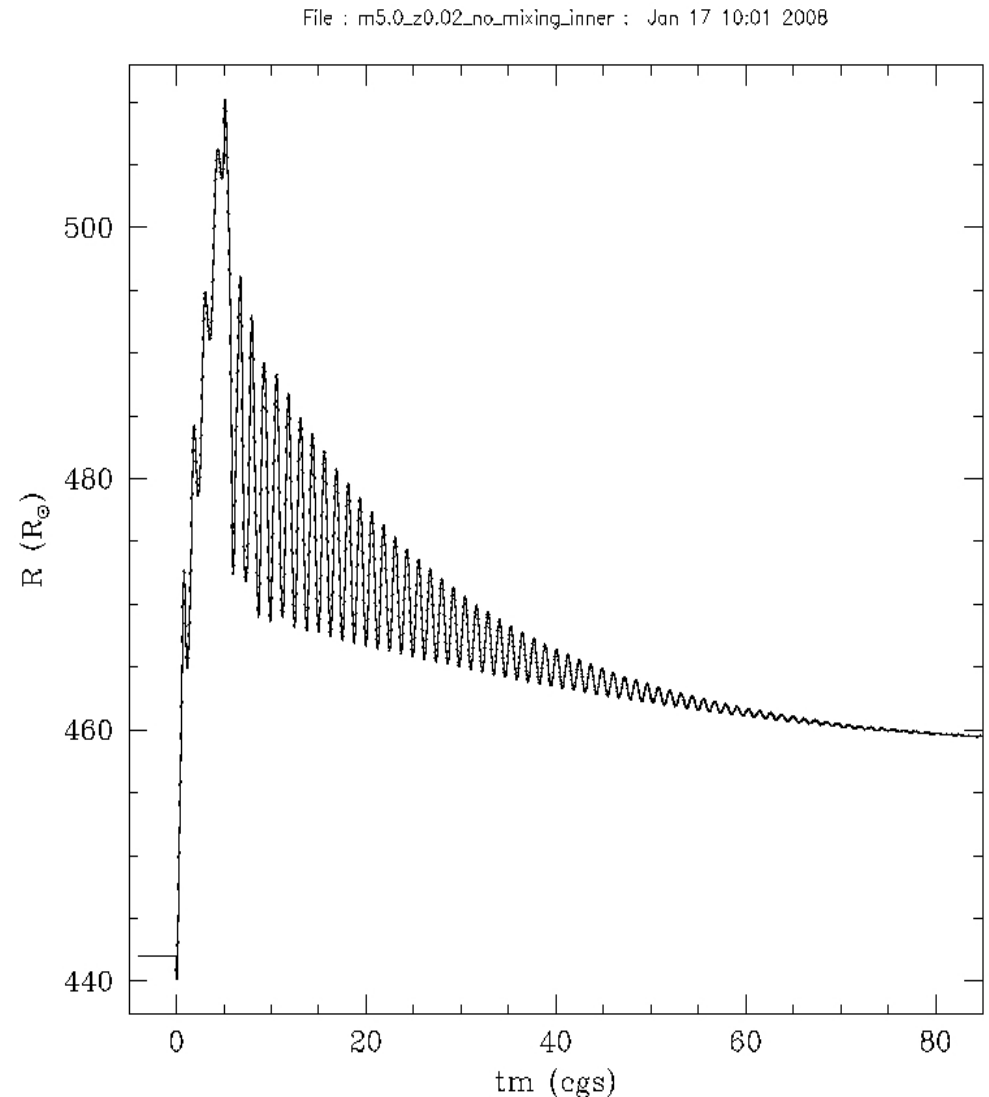
# Obtaining $\zeta_{AGB}$ by STAREVOL

- $\zeta_{AGB}$  calculate by polytropic models which not taking the star's structure into account.

- $$\zeta_{AGB} = \frac{d \ln R_R}{d \ln M} = -0.3 = \zeta_{polytrope}$$

Ritter (1999)

- Future study:  
 $\zeta_{AGB}$  for  $\neq M_{envelope}$ ,  $\neq M_*$   
and at  $\neq$  phases.



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