

# Formation of giant planetary systems:

## *Planet-planet interactions during the gas phase*

**S. Sotiriadis\***, A.-S. Libert

*naXys, Department of Mathematics, University of Namur*

*Joint work with B. Bitsch (Lund Observatory)*

*A. Crida (Nice Observatory)*

# Planetary system architecture

- Observations: the orbits of extrasolar systems are **more various** than the circular and coplanar ones of the Solar system

# Planetary system architecture

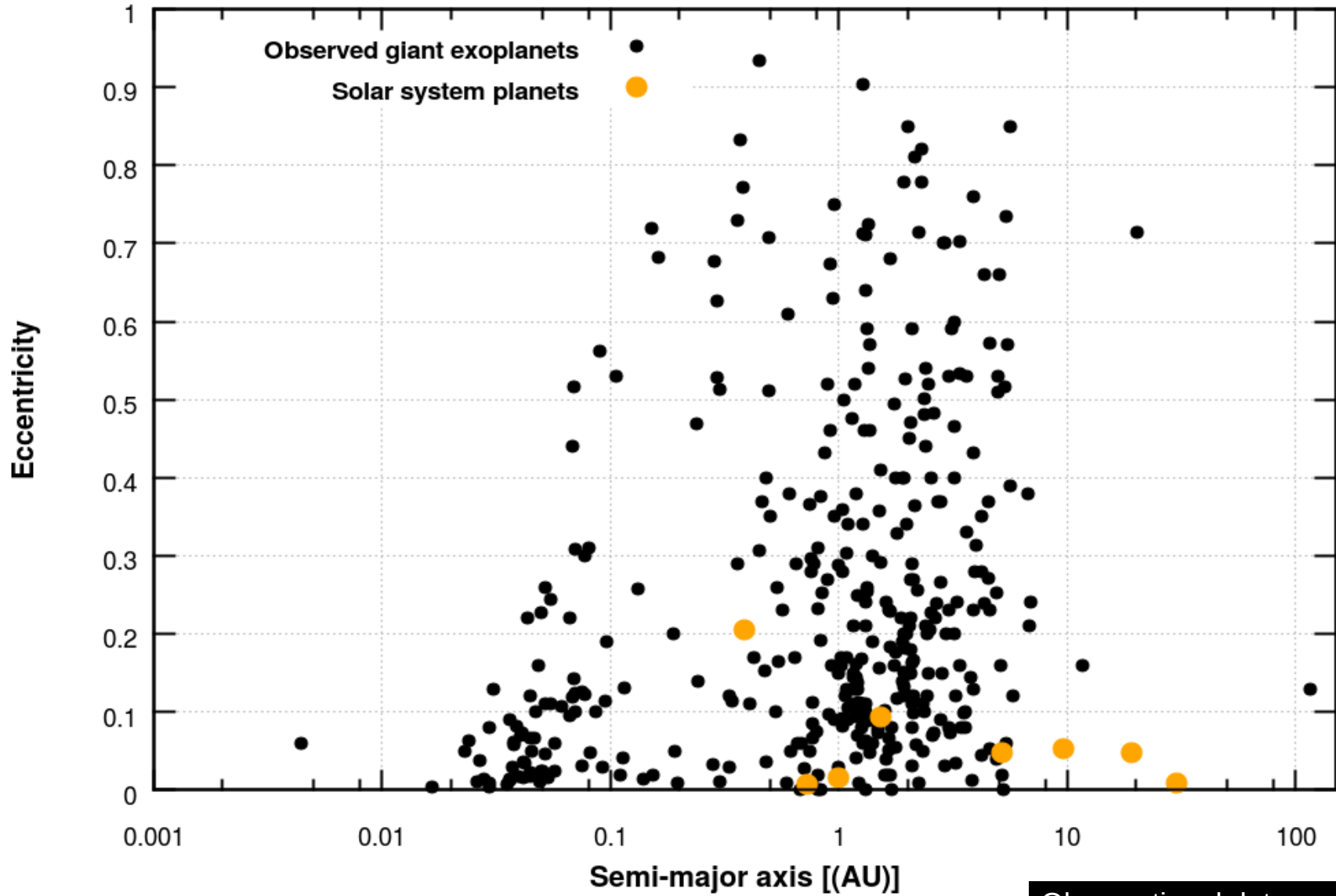
- Observations: the orbits of extrasolar systems are **more various** than the circular and coplanar ones of the Solar system

In particular, **RV-detected giant planets:**

- **Very diversified eccentricities**

# Eccentricity

Semi-major axis vs Eccentricity /  $M_p > 0.6 M_{\text{Jupiter}}$



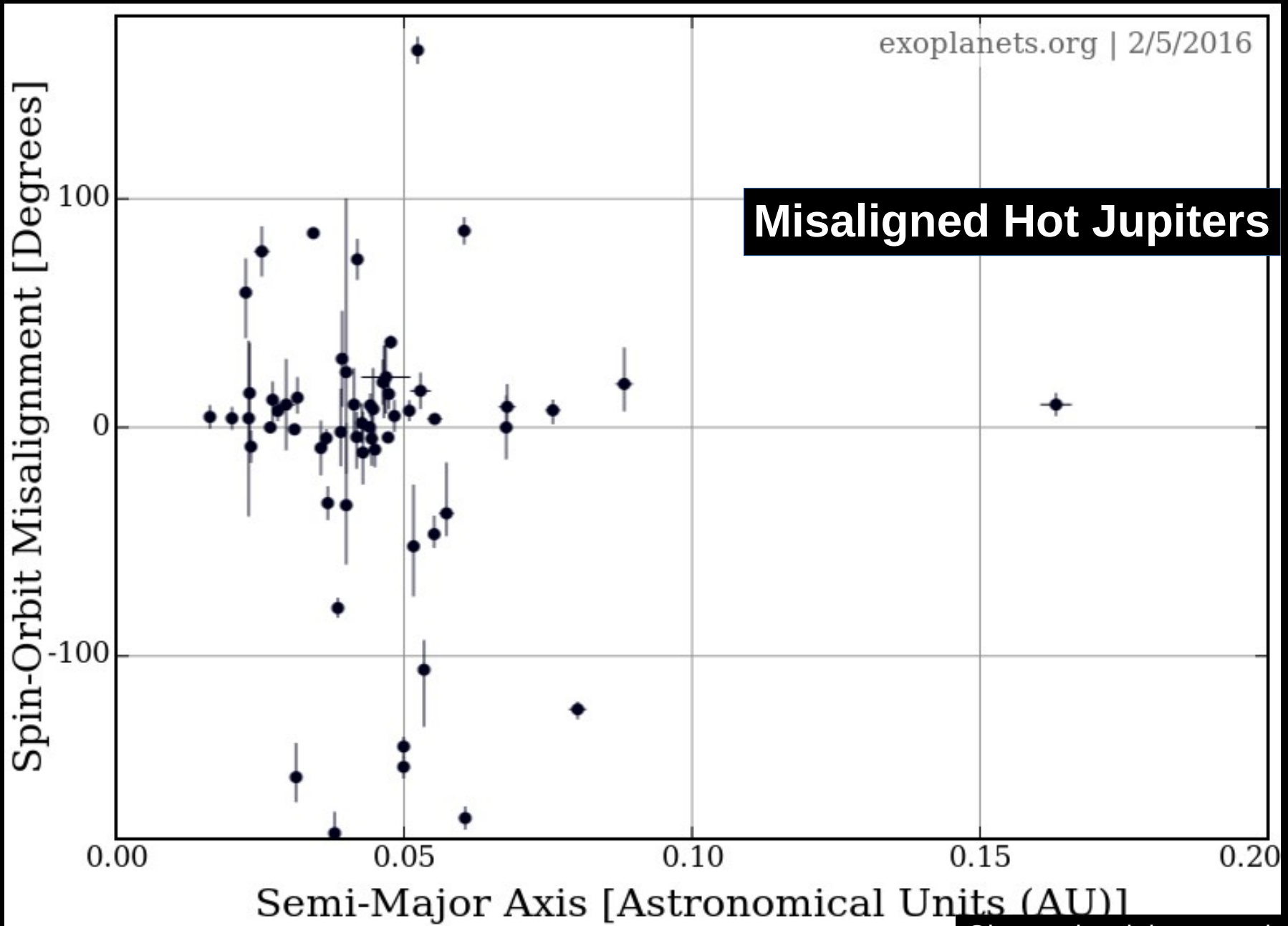
# Planetary system architecture

- Observations: the orbits of extrasolar systems are **more various** than the circular and coplanar ones of the Solar system

In particular, **RV-detected giant planets:**

- **Very diversified eccentricities**
- **Mutual inclinations unknown**

# *Inclinations: some clues*

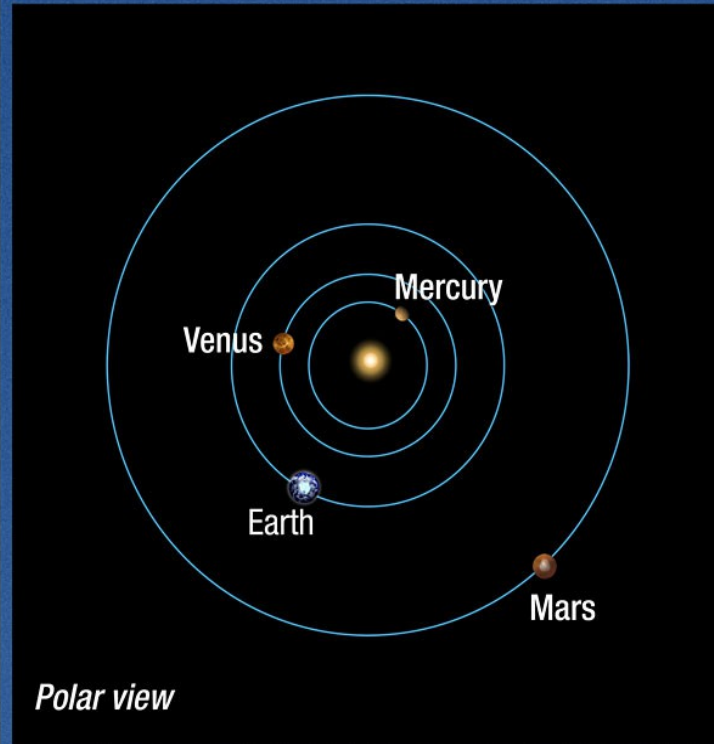


# Comparison of Solar System with Upsilon Andromedae System

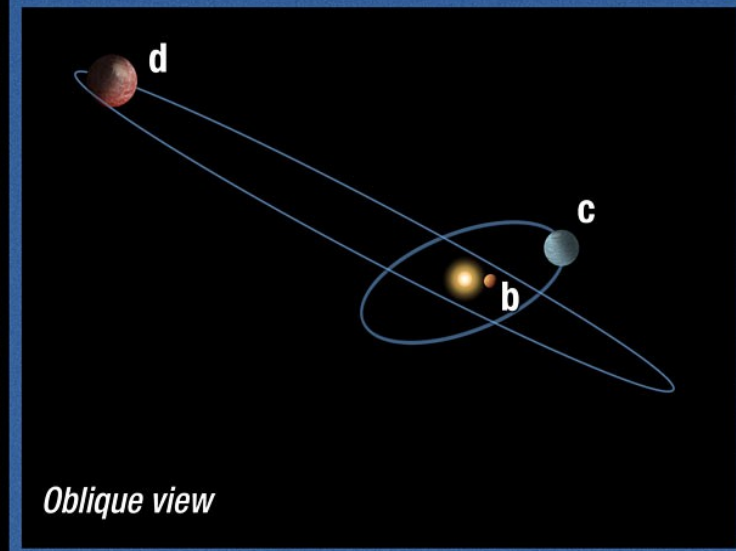
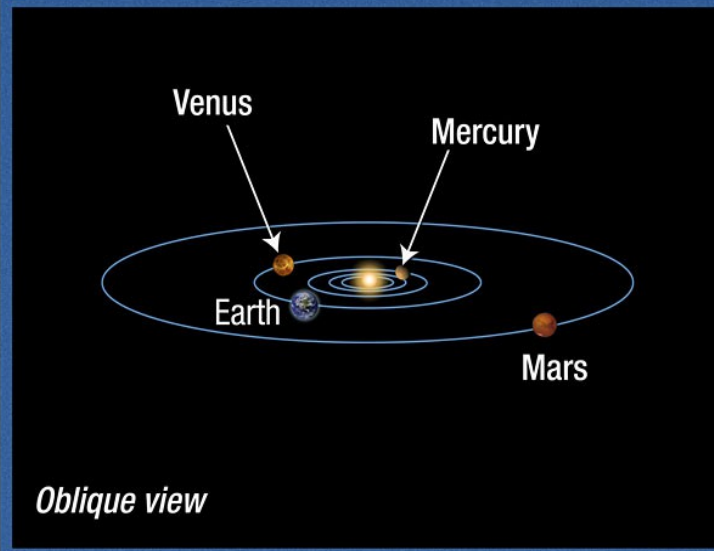
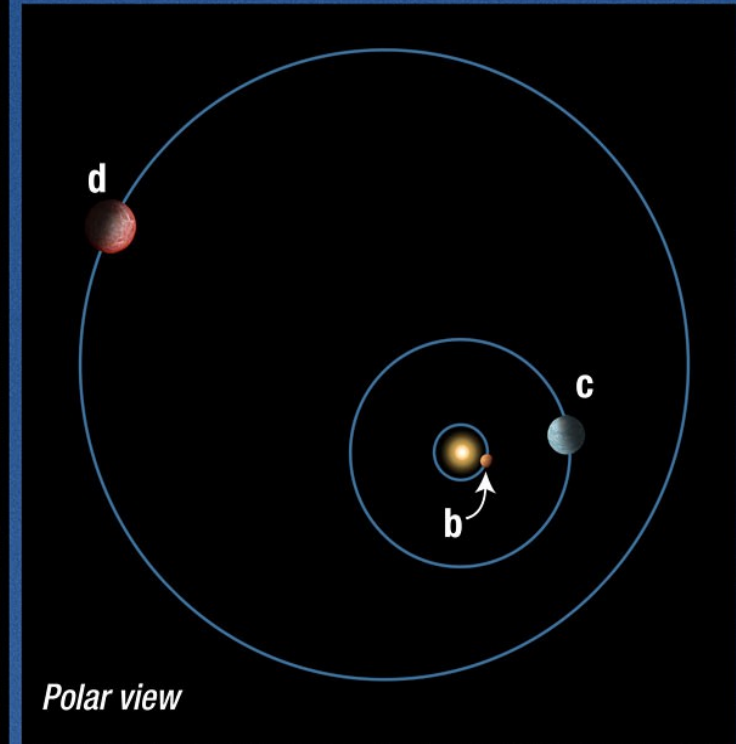
## $\upsilon$ Andromedae System

Mutual Inclination between  
c & d orbits  $\sim 30^\circ$

### Inner Solar System



### Upsilon Andromedae System



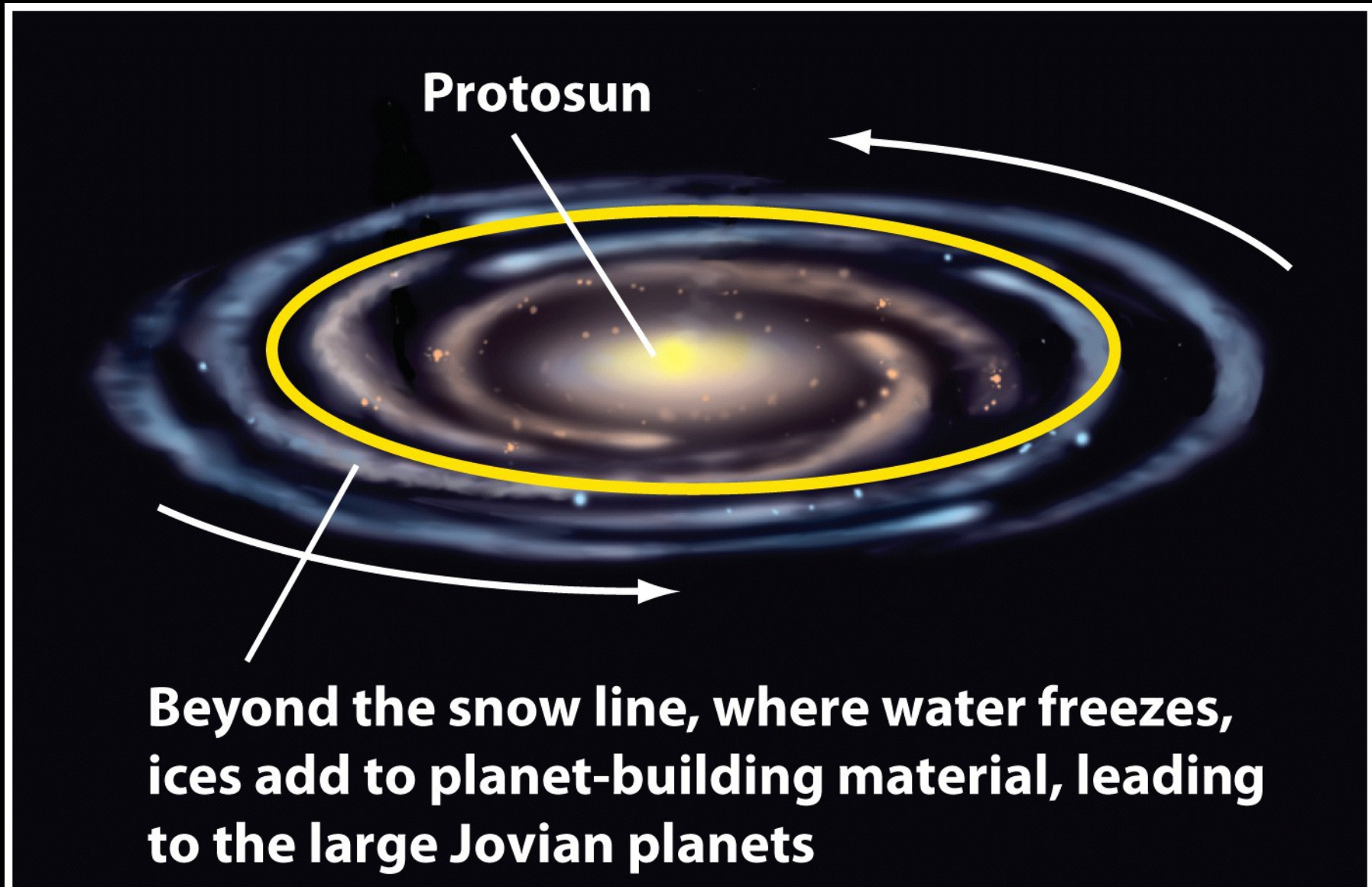
# Planetary system architecture

- Observations: the orbits of extrasolar systems are **more various** than the circular and coplanar ones of the Solar system
  - In particular, **RV-detected giant planets**:
    - **Very diversified eccentricities**
    - **Mutual inclinations unknown**
- **GOAL**: How to explain the formation of the RV-detected giant planet systems?



# Planet formation

- Gas giants form:
- Outside the “snow-line”
  - **Circular and co-planar orbits**



# Late-stage formation of giant planetary systems

- **STAGE I** / During the disc phase: **Giant planet migration** (Type II)  
(*e.g. Lin & Papaloizou 1986a, Kley 2000, Nelson et al. 2000*)
  - Eccentricity and inclination excitations  
(*e.g. Thommes & Lissauer 2003, Libert & Tsiganis 2009, Teyssandier & Terquem 2014*)
- **STAGE II** / After the disc phase: **Planet-planet scattering**  
(*e.g. Weidenschilling & Marzari 1996, Ford & Rasio 2008, Juric & Tremaine 2008, Chatterjee et al. 2008*)
  - Eccentricity and inclination excitations (*e distribution fits to observations*)  
BUT → Initial conditions problem
- **Combined action** of both previous mechanisms:  
Planet-planet interactions DURING migration in the protoplanetary disc  
(*e.g. Adams & Laughlin 2003, Matsumara et al. 2010, Libert & Tsiganis 2011*)

# Model description

Previous n-body studies

**1<sup>st</sup> order approximation  
for eccentricity damping**

$$\frac{\dot{e}}{e} = -K \frac{\dot{a}}{a}$$

**No effect of the disc on the  
Inclinations of the planets**

$$\frac{\dot{I}}{I} = ?$$

# Model description

## Bitsch et al. 2013: 3D Hydrodynamical simulations

Averaged torques acting on the planet in every orbit

Damping formulae for  $e$  and  $i$  (valid for  $e < 2/3$ , strong damping)  
 Suitable for ***n-body simulations*** → ***in our model***

### ECC

$$\mathcal{F}_e(i_P) = -\frac{M_{\text{disc}}}{0.01 M_{\star}} \left( a(i_P + i_D)^{-2b} + c i_P^{-2d} \right)^{-1/2}$$

$$\mathcal{G}_e(i_P, M_P, e_P) = 12.65 \frac{M_P M_{\text{disc}}}{M_{\star}^2} e_P \exp\left(-\left(\frac{i_P/1^\circ}{\tilde{M}_P}\right)^2\right)$$

$$a_e(M_P, e_P) = 80 e_P^{-2} \exp(-e_P^2 \tilde{M}_P / 0.26) 15^{\tilde{M}_P} (20 + 11 \tilde{M}_P - \tilde{M}_P^2)$$

$$b_e(M_P) = 0.3 \tilde{M}_P$$

$$c_e(M_P) = 450 + 2^{\tilde{M}_P}$$

$$d_e(M_P) = -1.4 + \sqrt{\tilde{M}_P} / 6.$$

### INCL

$$a_i(M_P, e_P) = 1.5 \times 10^4 (2 - 3e_P) \tilde{M}_P^3$$

$$b_i(M_P, e_P) = 1 + \tilde{M}_P e_P^2 / 10$$

$$c_i(M_P, e_P) = 1.2 \times 10^6 / \left[ (2 - 3e_P) \left( 5 + e_P^2 (\tilde{M}_P + 2)^3 \right) \right]$$

$$d_i(e_P) = -3 + 2e_P$$

$$g_i(M_P, e_P) = \sqrt{3 \tilde{M}_P / (e_P + 0.001)} \times 1^\circ$$

$$\mathcal{F}_i(M_P, e_P, i_P) = -\frac{M_{\text{disc}}}{0.01 M_{\star}} \left[ a_i \left( \frac{i_P}{1^\circ} \right)^{-2b_i} \exp(-i_P/g_i)^2 / 2 \right. \\ \left. + c_i \left( \frac{i_P}{40^\circ} \right)^{-2d_i} \right]^{-1/2}.$$

# Model description

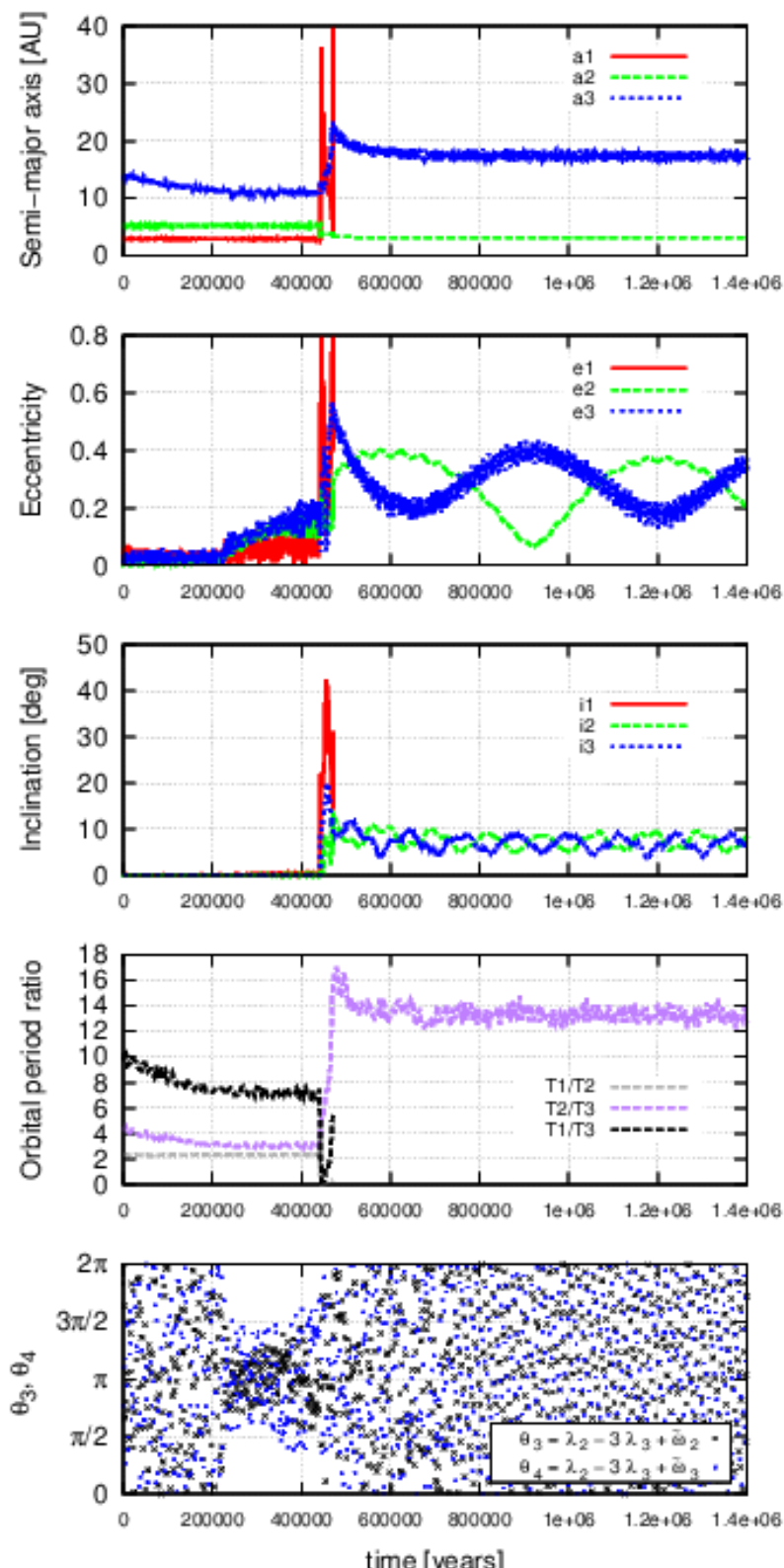
- **11000 simulations of 3 giant planet systems** in the late stage of the disc (SyMBA,  $2 \times 10^5$  computational hours (*CECI clusters*))
- **Type-II migration + improved damping effect** (Bitsch et al. 2013)
- Planets with mass in  $[1, 10] M_{\text{Jup}}$  initially outside the snowline, on quasi-circular and coplanar orbits
- **Different initial system configurations, planetary mass ratios, disc masses** ( $M_{\text{disc}}$  in  $[4, 32] M_{\text{Jup}}$ )
- Exponential decrease of the disc mass, with a dispersal time of  $\sim 1$  Myr

# Objectives

- Impact of the eccentricity and inclination damping on the final system configurations (a – e – I)
- If non-coplanar systems, identification of dynamical mechanisms producing inclination increase

# Dynamical mechanisms for inclination increase

## Planet – planet scattering during the gas phase

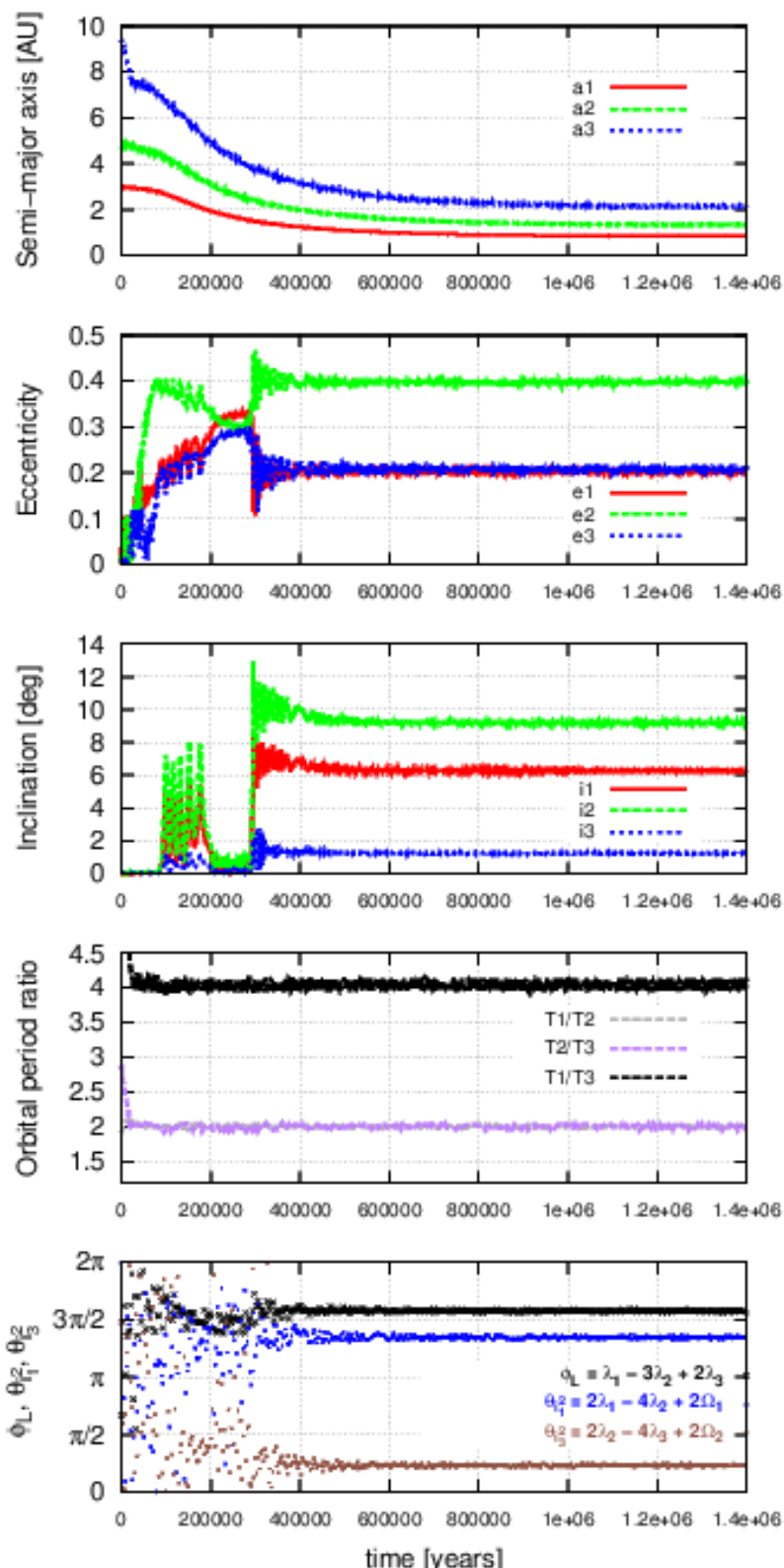


- 1:3 MMR capture for the outer planets
- Subsequent increase of eccentricities
- When the inner pair approaches the 3:7 commensurability, destabilization of the whole system
- Ejection of the inner less massive body
- Remaining planets in inclined orbits with large eccentricity variations and large orbital separation



# Dynamical mechanisms for inclination increase

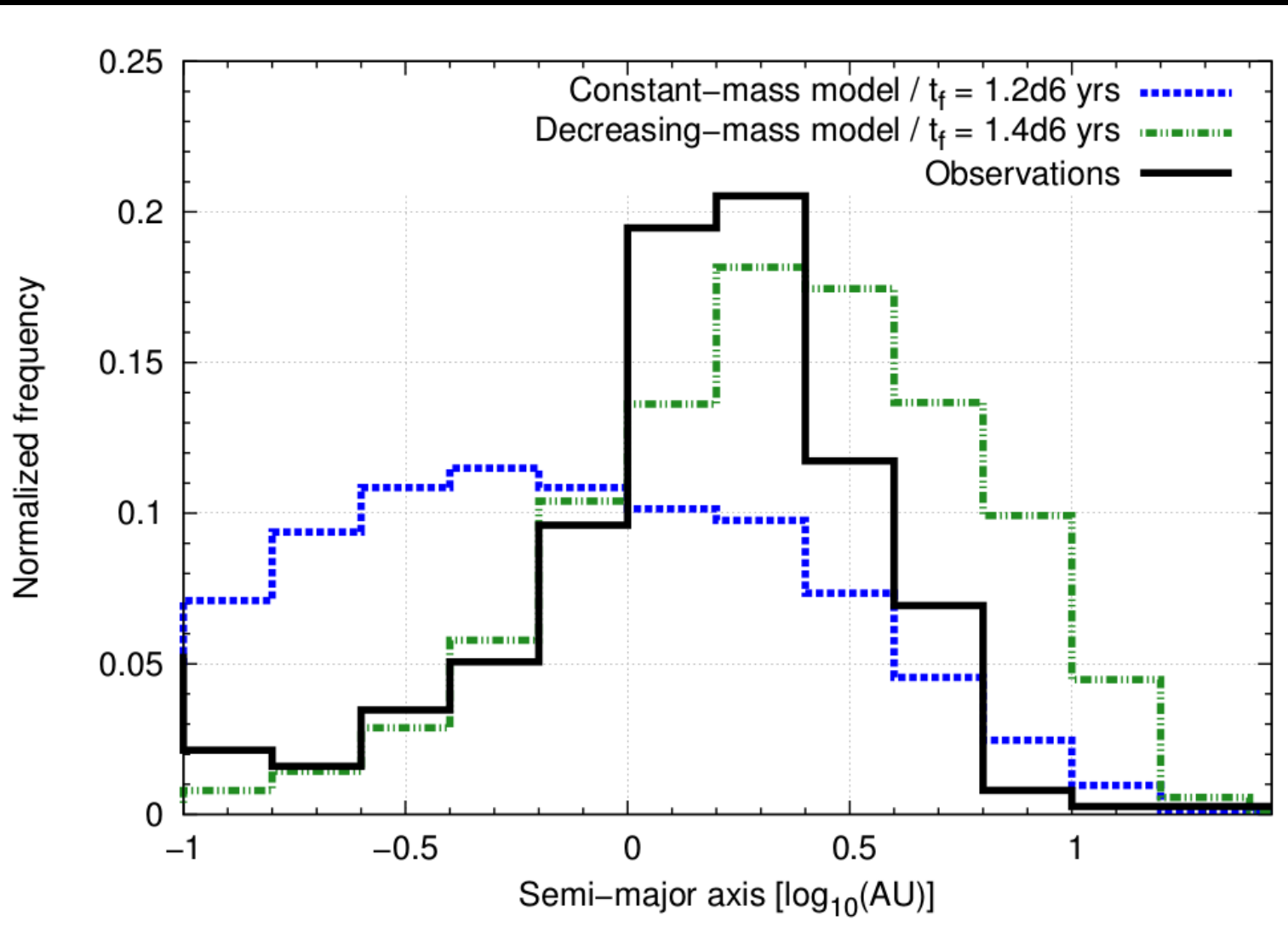
## Three-body mean-motion resonance



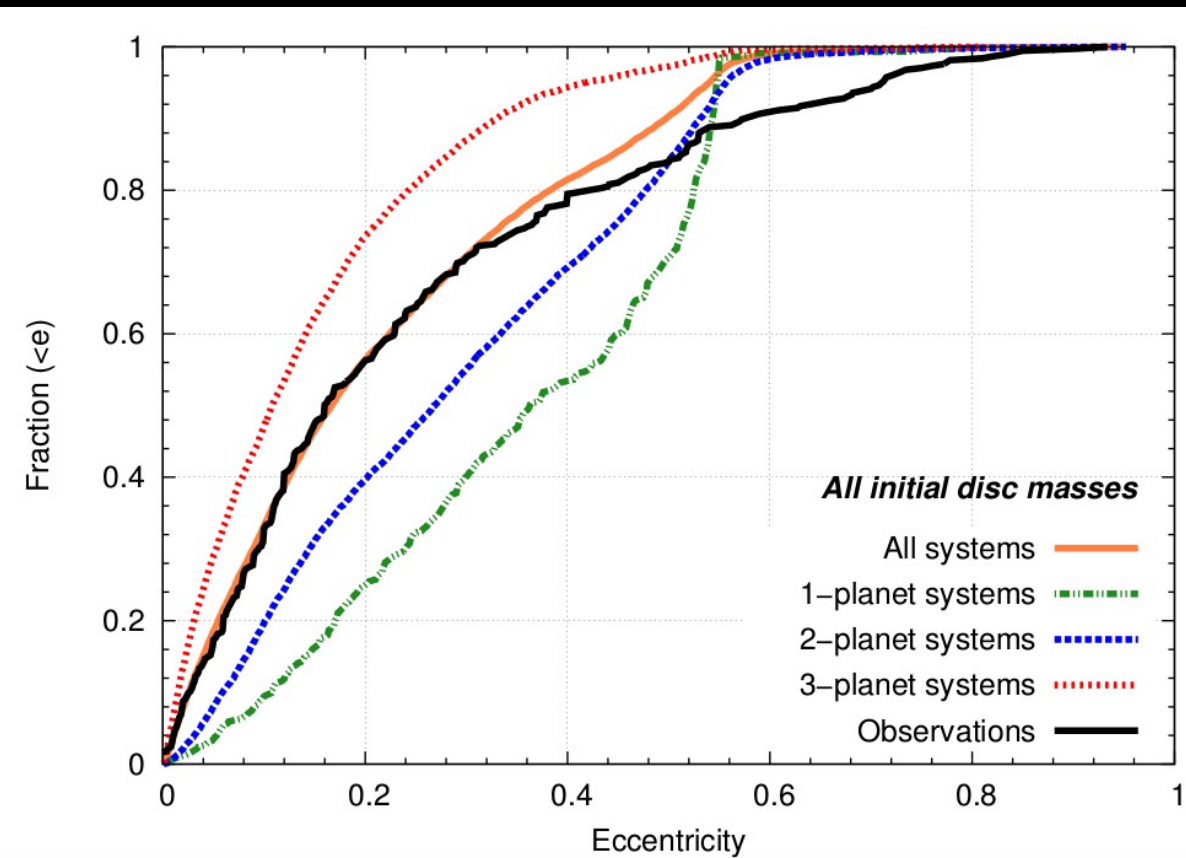
- Capture in a 1:2:4 Laplace resonance
- Subsequent increase of the eccentricities
- When the eccentricities are high enough, inclination-type resonance
- Strong damping: planets back to the midplane
- Exponential decay of the gas disc: inclination-type resonance produces high inclinations maintained for a long time



# Semi-major axis distribution

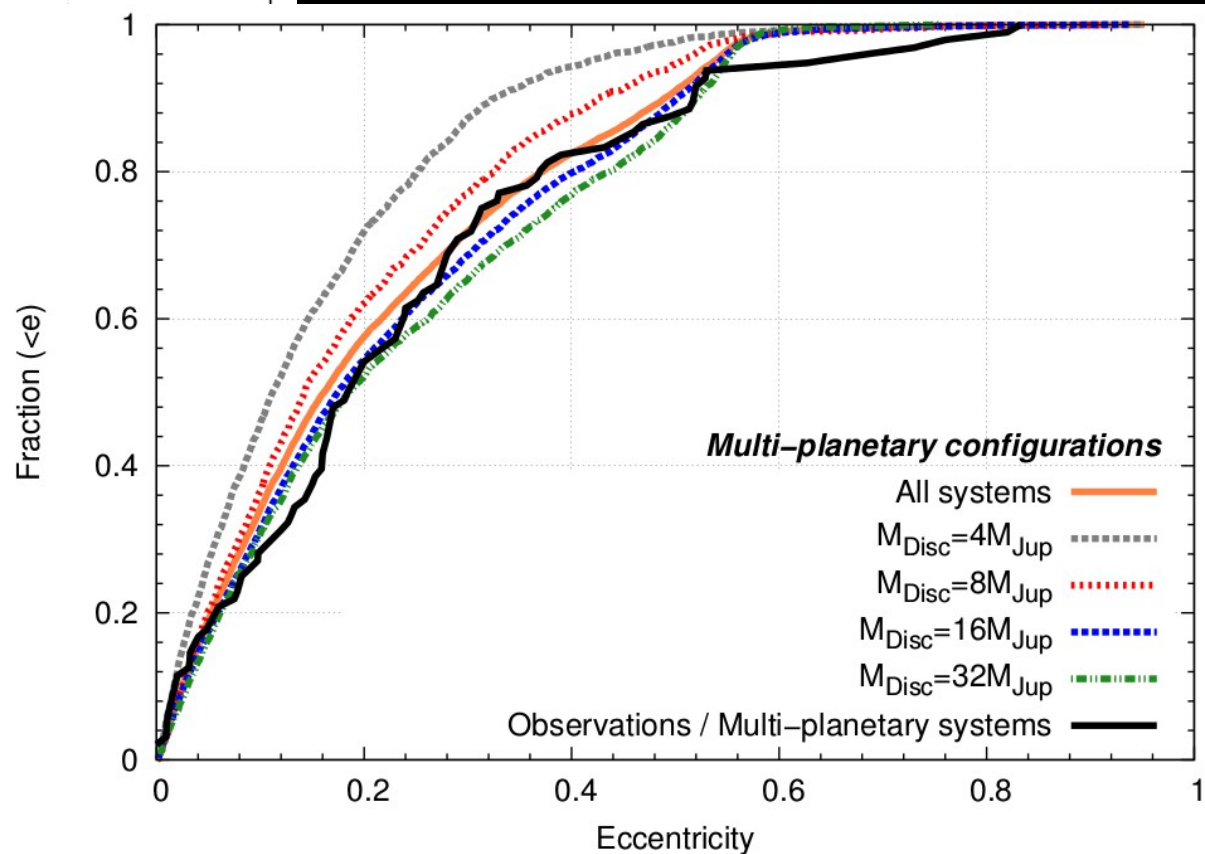
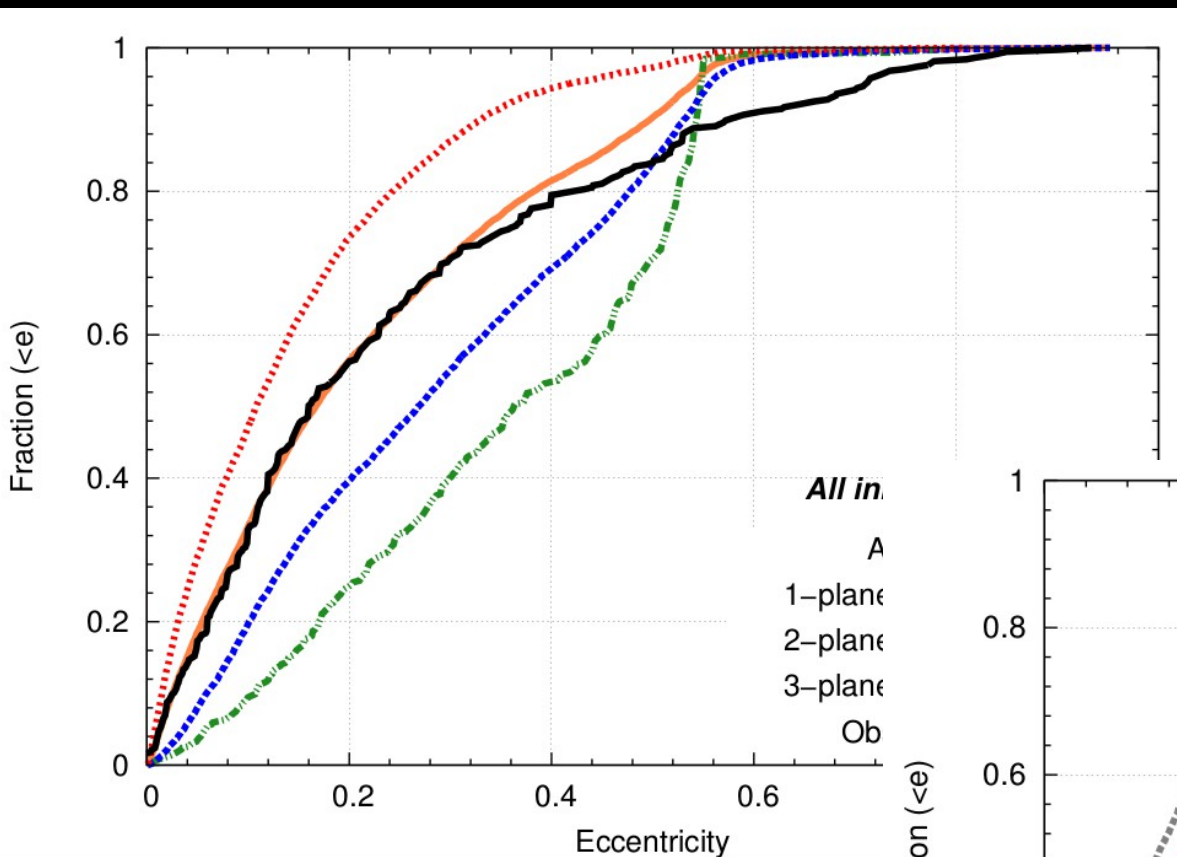


# Eccentricity distribution



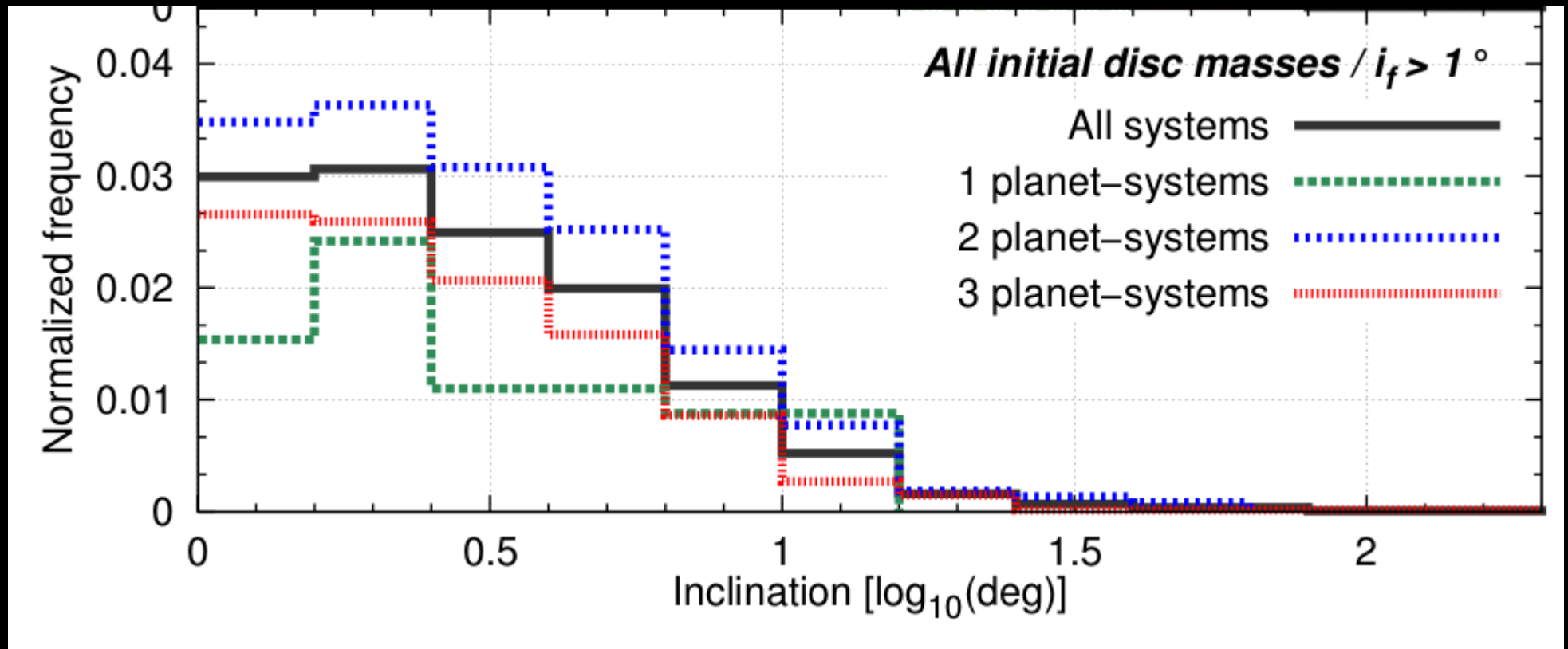
Perfect agreement up to 0.35,  
lack of highly eccentric orbits

# Eccentricity distribution



When removing single planet systems, good agreement up to 0.55

# Inclination distribution

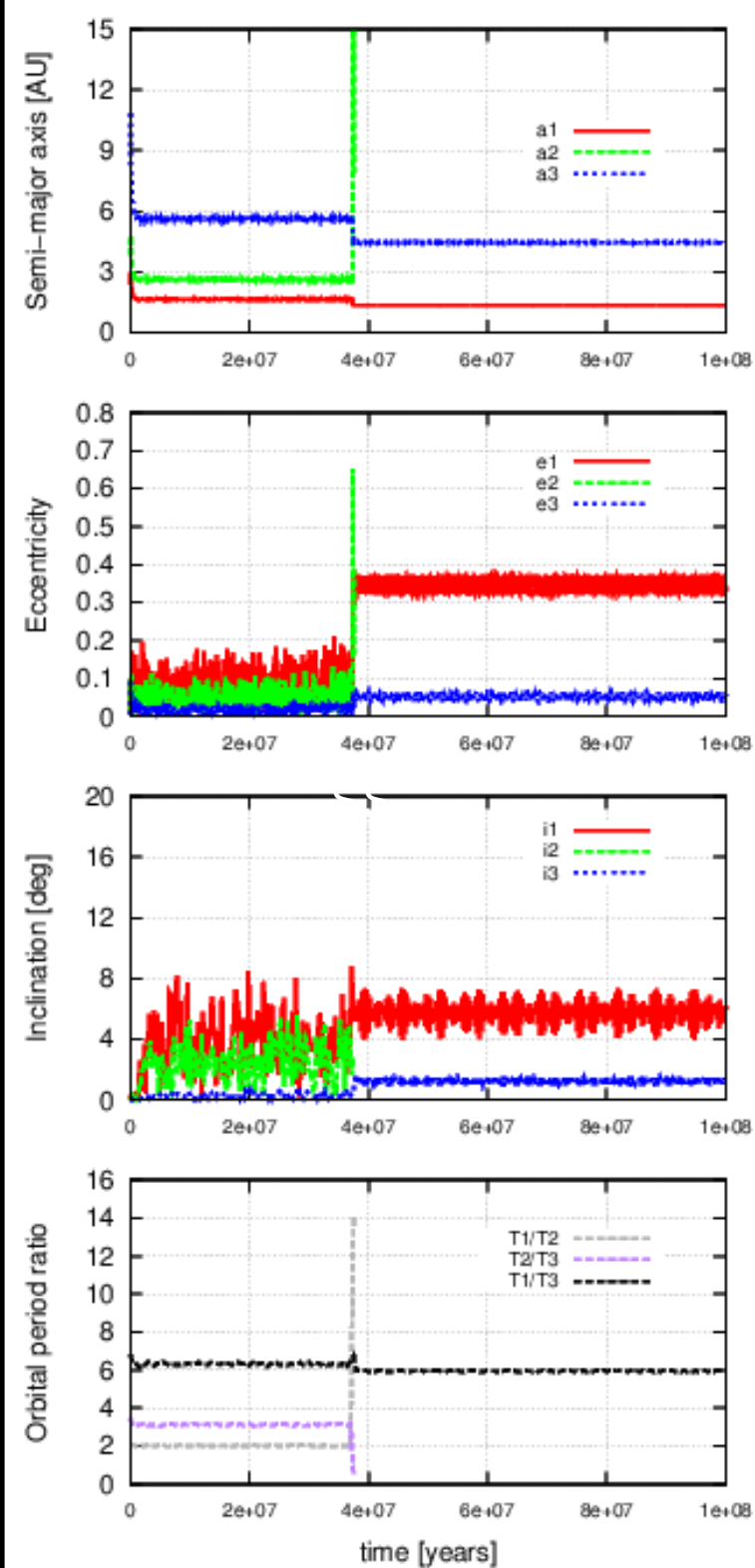


**3% of the systems have mutual inclination  $> 10^\circ$   
at the dispersal of the disc**

# Long-term evolution

- Orbital adjustments due to planet-planet interactions can occur on a longer timescale AFTER the disc phase
- Additional subset  
Integration up to 100 Myrs
- Number of planets at 1.4d6 and 1d8

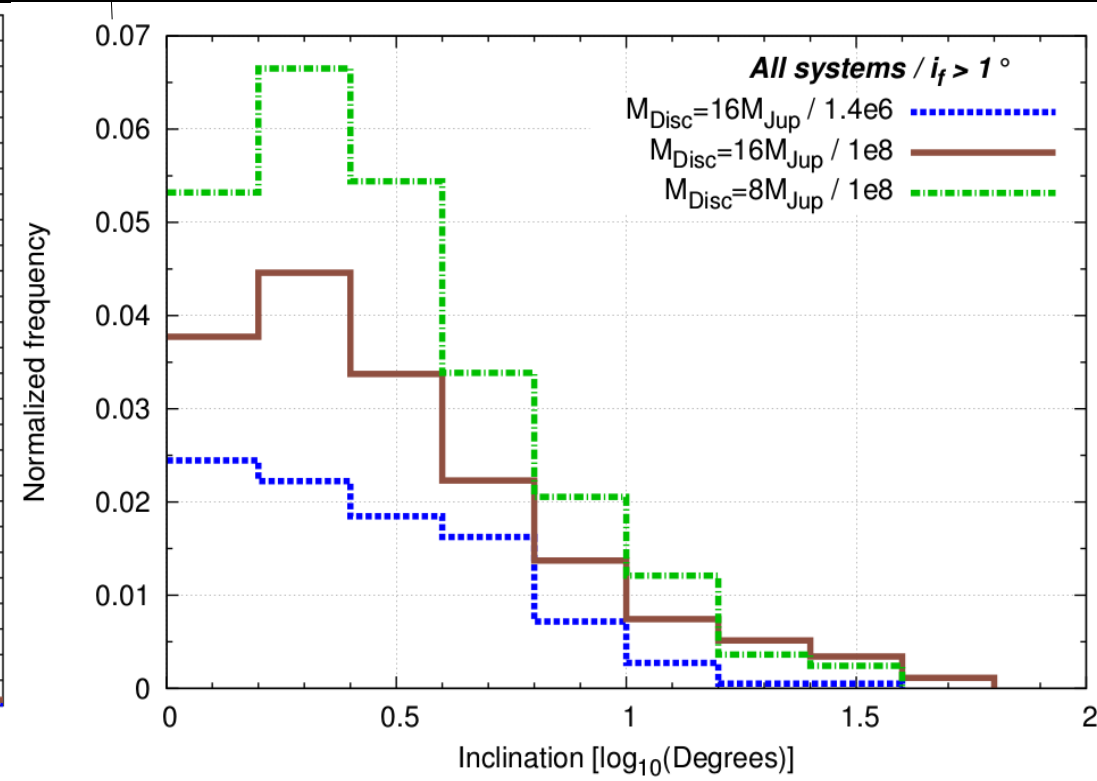
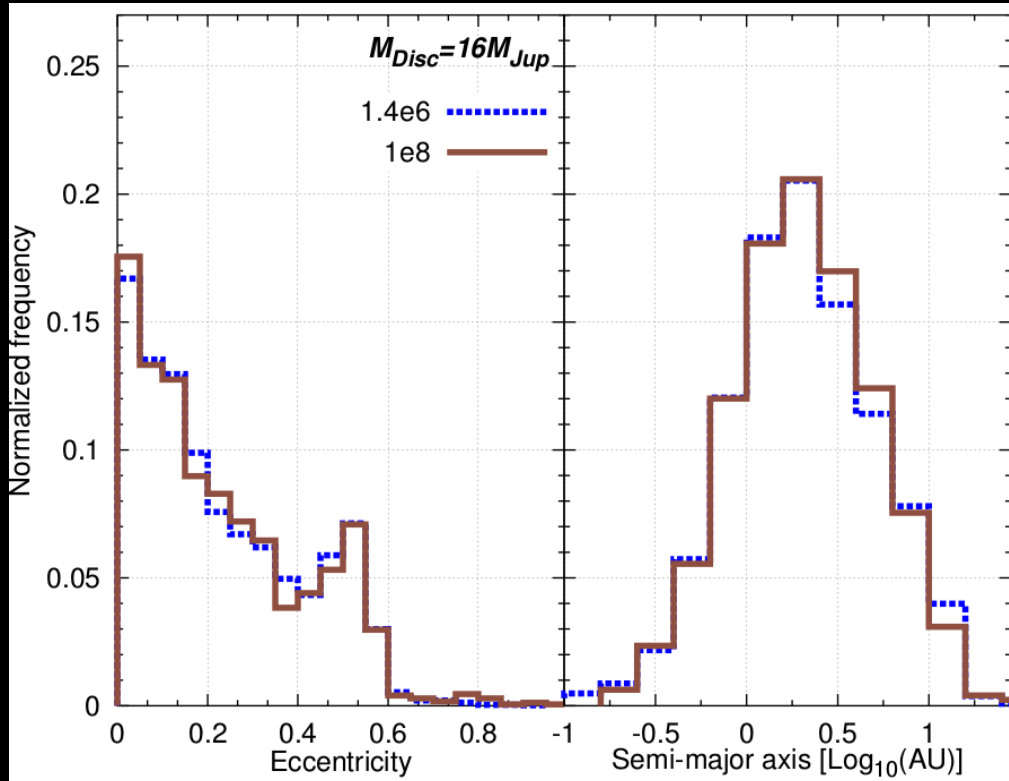
	1 planet	2 planets	3 planets
1.4d6 yrs	7 %	50 %	40 %
1d8 yrs	12 %	53 %	32 %



# Long-term evolution

No significant change on the semi-major axis and eccentricity distributions

5% of the systems have mutual inclination  $> 10^\circ$  on long-time scale



# Summary

- **Good agreement** between our simulations and the observed population of extrasolar systems
- ***Eccentricities well-diversified*** at the dispersal of the disc, despite the strong damping exerted by the disc
- Very efficient damping exerted by the disc on the inclinations: ***most of the planets end up in the midplane***
- Inclination-type resonance and planet-planet scattering events during/after the gas phase induce inclination excitation: ***5% of highly mutually inclined systems (>10°) in our population***
- Future observations: percentage of inclined systems could help to discriminate between the formation scenarios

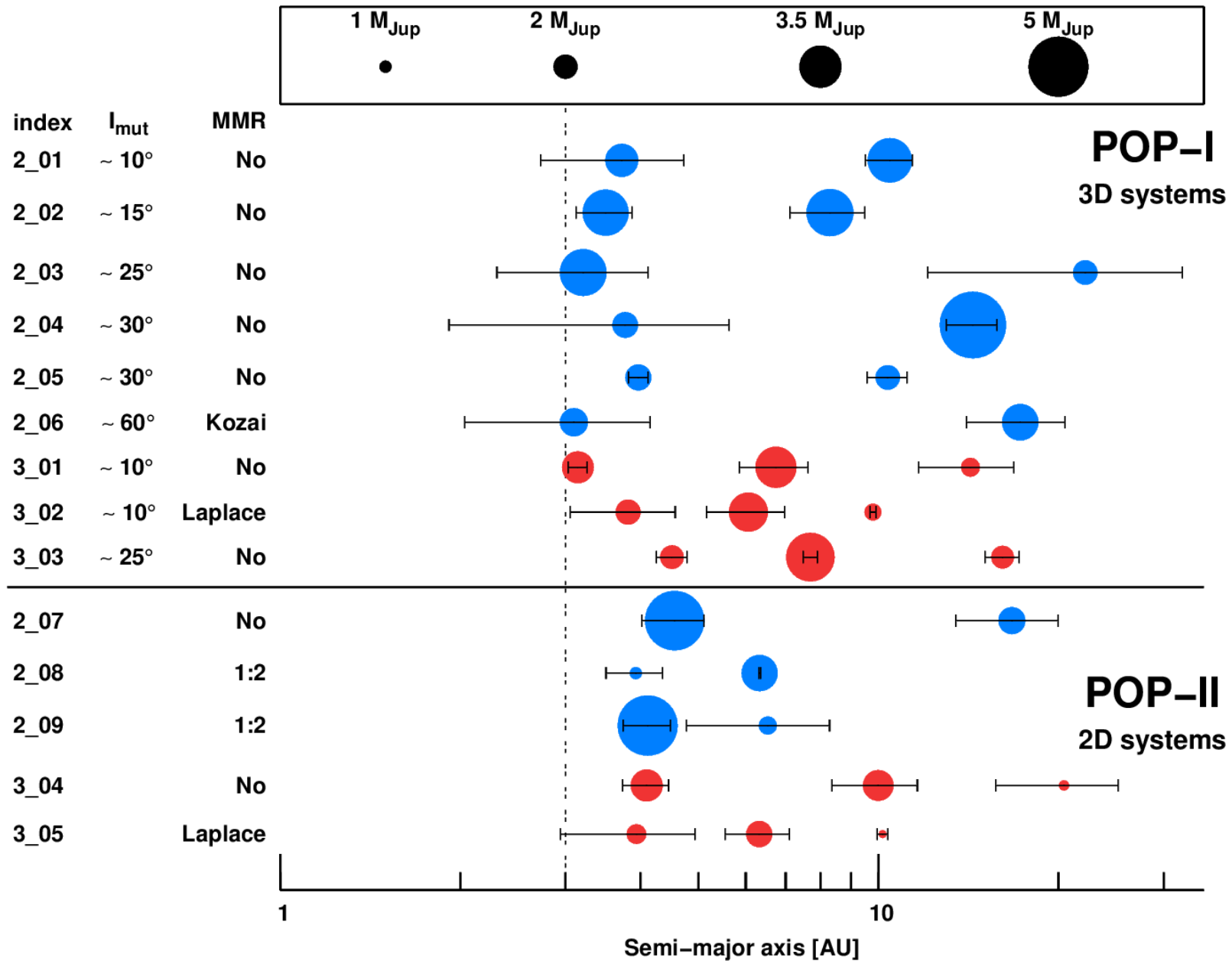
# Next step: Terrestrial planet formation

What is the impact of the **eccentric and inclined** giant planet population on the **terrestrial planet formation** process?



# Terrestrial planet formation

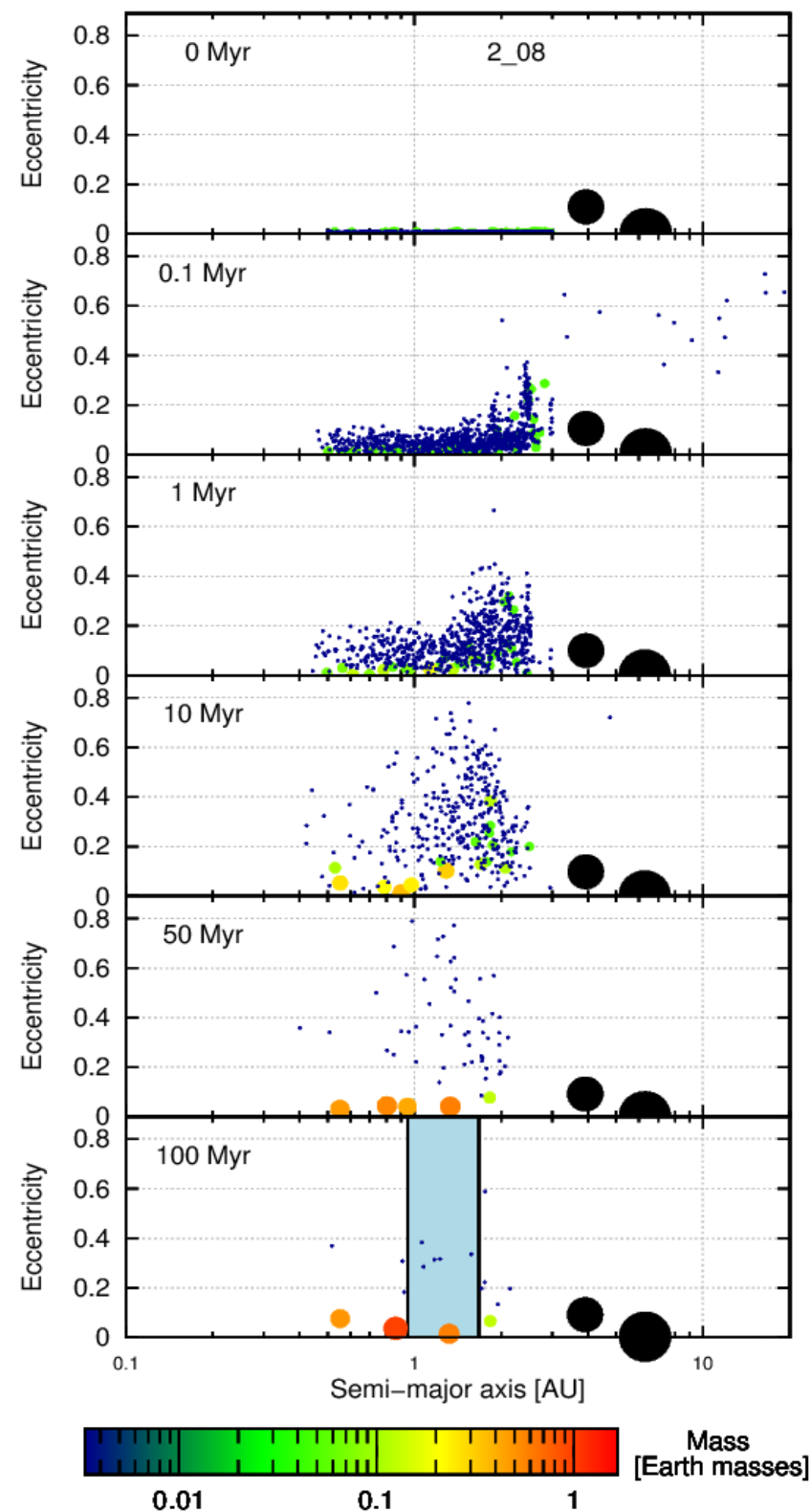
Initial conditions for our simulations



# Terrestrial planet formation

## Preliminary results

- Semi-major axis vs **eccentricity** for a co-planar system (POP-II) initially in a 2:1 MMR
- We have 4 Earth-like planets in near-circular orbits
- One of them inside the habitable zone



# Terrestrial planet formation

## Preliminary results

- Semi-major axis vs **inclination** for a 3D system (POP-I)
- Giants with initial  $I_{\text{mut}} = 30^\circ$
- At 100 Myrs, one planet with 0.2 Earth's mass inside the habitable zone with  $\langle I \rangle \sim 25^\circ$

Formation of inclined terrestrial planets is possible with the classical accretion theory

**TO BE CONTINUED**

